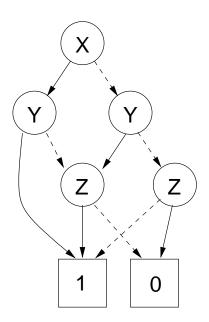
BuDDy: Binary Decision Diagram package Release 2.2

Jørn Lind-Nielsen IT-University of Copenhagen (ITU) e-mail: buddy@itu.dk November 9, 2002



Contents

1	Introduction
	1.1 Acknowledgements
2	Users Guide
	2.1 Getting BuDDy
	2.2 Installing
	2.3 Compiling
	2.4 Programming with BuDDy
	2.4.1 More Examples
	2.5 Variable sets
	2.6 Dynamic Variable Reordering
	2.7 Error Handling
	2.8 The C++ interface
	2.9 Finite Domain Blocks
	2.10 Boolean Vectors
	2.10.1 C++ Interface
	2,10,1 0 1,10,011,000
3	Efficiency Concerns
1	Some Implementation details
5	Reference
	bddCacheStat
	bddGbcStat
	$\mathrm{bddStat}$
	$\operatorname{bdd_addref}$
	bdd_addvarblock
	bdd_intaddvarblock
	bdd_allsat
	bdd_and
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
	bdd_appall
	bdd_appex
	bdd_apply
	bdd_appuni
	bdd_autoreorder
	bdd_autoreorder_times
	bdd_biimp
	bdd_blockfile_hook
	bdd buildcube

odd_ibuildcube		. 29
$\operatorname{odd_cachestats}$. 30
odd_clear_error		. 30
odd_clrvarblocks		. 30
$\operatorname{odd_compose}$. 31
$\operatorname{odd_constrain}$. 31
$\operatorname{odd_delref}$. 32
odd_disable_reorder		. 32
$\operatorname{odd}_{\operatorname{\mathbf{d}one}}$. 32
odd_enable_reorder		
odd_error_hook		
odd_errstring		
odd_exist		
odd_extvarnum		
odd_false		
odd_file_hook		
odd_forall		
odd_freepair		
pdd _fullsatone		
$\operatorname{pdd_gbc_{hook}}$		
$\operatorname{pdd}_{\operatorname{gbe}}$ and $\operatorname{gbe}_{\operatorname{abs}}$		
odd_getnodenum		
odd_getreorder_method		
pdd getreorder_times		
odd_high		
odd_imp		
odd_init		
odd_isrunning		
odd_ite		
odd_ithvar		
odd_level2var		
odd_load		
odd_fnload		
odd_low		
odd_makeset	-	. 43
odd_newpair	٠	. 44
odd_nithvar		. 44
odd_nodecount	•	
odd_not		
odd_or		
$\operatorname{pathcount}$. 46
odd_printall		. 46
odd_fprintall		. 46
odd_printdot		. 47
odd_fprintdot		. 47
$\operatorname{odd_printorder}$. 47
$\operatorname{printset}$. 48
$\operatorname{pdd_fprintset}$. 48
$\operatorname{printstat}$		
$\operatorname{printstat}$		

bdd_printtable			49
bdd_fprinttable			49
bdd_relprod			49
bdd_reorder			50
bdd_reorder_gain			51
bdd_reorder_hook			51
bdd_reorder_probe			52
bdd_reorder_verbose			52
$bdd_replace \ . \ . \ . \ . \ . \ . \ . \ . \ . \ $			53
bdd_resetpair			53
bdd_resize_hook			54
bdd_restrict			55
bdd_satcount			55
bdd_setcountset			55
bdd_satcountln			56
bdd_setcountlnset			56
bdd_satone			56
bdd_satoneset			57
bdd_save			57
bdd_fnsave			57
bdd_scanset			58
bdd_setcacheratio			58
bdd_setmaxincrease			59
bdd_setmaxnodenum			59
bdd_setminfreenodes			60
bdd_setpair			60
bdd_setbddpair			60
bdd_setpairs			61
bdd_setbddpairs			61
bdd_setvarnum			61
bdd_setvarorder			62
bdd_simplify			62
bdd_stats			62
bdd_strm_hook			63
bdd_support			63
bdd_swapvar			64
bdd_true			64
bdd_unique			65
bdd_var			65
bdd_var2level			65
bdd_varblockall			66
bdd_varnum			66
bdd_varprofile			66
bdd_veccompose			67
bdd_versionnum			67
bdd_versionstr			67
bdd_xor			68
bddfalse			68
bddtrue			68
hvec			69

$bvec_add \dots \dots$	69
$bvec_addref \ \dots $	70
$bvec_coerce \ \dots $	70
$bvec_con \dots $	70
$bvec_copy \ \dots $	71
$bvec_delref \dots $	71
$bvec_div \dots $	71
$bvec_divfixed \dots \dots$	72
$bvec_equ \dots $	72
$bvec_false \ \dots $	72
$bvec_free \dots \dots$	73
bvec_gte	73
$bvec_gth \dots $	73
$bvec_isconst \qquad \dots $	74
$bvec_ite $	74
bvec_lte	74
$bvec_lth \ldots \ldots$	75
bvec_map1	75
bvec_map2	76
bvec_map3	76
bvec_mul	77
bvec_mulfixed	77
bvec_neq	77
bvec_shl	78
bvec_shlfixed	78
bvec_shr	79
bvec_shrfixed	79
bvec_sub	80
bvec_true	80
bvec_val	81
bvec_var	81
$bvec_varfdd \dots $	82
bvec_varvec	82
$fdd_clearall \ \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$	82
$fdd_domain \ \dots $	83
$fdd_domainnum . \ . \ . \ . \ . \ . \ . \ . \ . \ .$	83
$fdd_domainsize \ \ldots \ $	83
$fdd_equals \dots $	84
$fdd_extdomain \dots \dots$	84
$fdd_file_hook $	85
$fdd_intaddvarblock \ . \ . \ . \ . \ . \ . \ . \ . \ . \ $	85
$fdd_ithset \ldots \ldots$	86
fdd_ithvar	86
$fdd_makeset . \ . \ . \ . \ . \ . \ . \ . \ . \ .$	87
$fdd_overlapdomain \ \ldots \ $	87
fdd_printset	88
	88
fdd_scanallvar	88
$fdd_scanset \dots \dots \dots \dots \dots \dots \dots \dots \dots $	89
fdd_scanvar	89

fdd_setpairs 90 fdd_strm_hook 91 fdd_varnum 91 fdd_vars 92 operator< 92	d_setpair	90
fdd_varnum	d_setpairs	90
$\mathrm{fdd_vars}$	d_strm_hook	91
	d_varnum	91
operator<<	d_{vars}	92
	perator<<	92

Introduction

BuDDy is a Binary Decision Diagram package that provides all of the most used functions for manipulating BDDs. The package also includes functions for integer arithmetics such as addition and relational operators.

BuDDy started as a technology transfer project between the Technical University of Denmark and Bann Visualstate. The later is now using the techniques from BuDDy in their software. See www.visualstate.com.

This manual describes only the interface to BuDDy, not the underlying theory of BDDs. More information about that can be found in Henrik Reif Andersen's "An Introduction To Binary Decision Diagrams" which is supplied with the BuDDY distribution. Even more information can of course be found in the original papers by Bryant, Rudell and Brace [1, 3, 2, 4]

1.1 Acknowledgements

Thanks to the following people for new ideas, bug hunts and lots of discussions: Gerd Behrmann, Henrik Reif Andersen, Ken Larsen, Jacob Lichtenberg, Poul Williams, Nikolaj Bjorner, Alan Mishchenko, Henrik Hulgaard, and Malte Helmert.

Users Guide

2.1 Getting BuDDy

BuDDy can be found on the server http://www.itu.dk/research/buddy.

2.2 Installing

- 1. Edit the file "config" to specify your compiler and install options.
- 2. Type make to make the binary.
- 3. Type make install to copy the BDD files to their appropriate directories
- 4. Type make examples to make the examples

2.3 Compiling

This is rather simple. Just inform the compiler of where the binaries and include files are installed. With Gnu C this is done with the -I and -L options. Assuming that the binary library libbdd.a is installed in /usr/local/lib and the include file bdd.h is installed in /usr/local/include, then the compile command should be

```
cc -I/usr/local/include myfile.c -o myfile -L/usr/include/lib -lbdd
```

If the above directories are included in your search path already, then you might be able to reduce the command to

```
cc myfile.c -o myfile -lbdd
```

2.4 Programming with BuDDy

First of all a program needs to call bdd_init(nodenum,cachesize) to initialize the BDD package. The nodenum parameter sets the initial number of BDD nodes and cachesize sets the size of the caches used for the BDD operators (not the unique node table). These caches are used for bdd_apply anmong others.

Good initial values are

Example	nodenum	${f cachesize}$
Small test examples	1000	100
Small examples	10000	1000
Medium sized examples	100000	10000
Large examples	1000000	variable

Too few nodes will only result in reduced performance as this increases the number of garbage collections needed. If the package needs more nodes, then it will automatically increase the size of the node table. Use bdd_setminfreenodes to change the parameters for when this is done and use bdd_setcacheratio to enable dynamical resizing of the operator caches. You may also use the function bdd_setmaxincrease to adjust how BuDDy resizes the node table.

After the initialization a call must be done to bdd_setvarnum to define how many variables to use in this session. This number may be increased later on either by calls to bdd_setvarnum or to bdd_extvarnum.

The atomic functions for getting new BDD nodes are bdd_ithvar(i) and bdd_nithvar(i) which returns references to BDD nodes of the form $(v_i, 0, 1)$ and $(v_i, 1, 0)$. The nodes constructed in this way corresponds to the positive and negative versions of a single variable. Initially the variable order is $v_0 < v_1 < ... < v_{n-1} < v_n$.

The BDDs returned from bdd_ithvar(i) can then be used to form new BDDs by calling bdd_apply(a,b,op) where op may be bddop_and or any of the other operators defined in bdd.h. The apply function performs the binary operation indicated by op. Use bdd_not to negate a BDD. The result from bdd_apply and any other BDD operator must be handed over to bdd_addref to increase the reference count of the node before any other operation is performed. This is done to prevent the BDD from being garbage collected. When a BDD is no longer in use, it can be de-referenced by a call to bdd_delref. The exceptions to this are the return values from bdd_ithvar and bdd_nithvar. These do not need to be reference counted, although it is not an error to do so. The use of the BDD package ends with a call to bdd_done. See the figures 2.1 and 2.2 for an example.

Information on the BDDs can be found using the bdd_var, bdd_low and bdd_high functions that returns the variable labelling a BDD, the low branch and the high branch of a BDD.

Printing BDDs is done using the functions bdd_printal1 that prints all used nodes, bdd_printtable that prints the part of the nodetable that corresponds to a specific BDD and bdd_printset that prints a specific BDD as a list of elements in a set (all paths ending in the true terminal).

2.4.1 More Examples

More complex examples can be found in the buddy/examples directory.

2.5 Variable sets

For some functions like bdd_exist it is possible to pass a whole set of variables to be quantified, using BDDs that represent the variables. These BDDs are simply the conjunction of all the variables in their positive form and can either be build that way or by a call to bdd_makeset. For the bdd_restrict function the variables need to be included in both positive and negative form which can only be done manually.

If for example variable 1 and variable 3 are to be included in a set, then it can be done in two ways, as shown in figure 2.3.

```
#include <bdd.h>
main(void)
{
   bdd x,y,z;

   bdd_init(1000,100);
   bdd_setvarnum(5);

   x = bdd_ithvar(0);
   y = bdd_ithvar(1);
   z = bdd_addref(bdd_apply(x,y,bddop_and));

   bdd_printtable(z);
   bdd_delref(z);
   bdd_done();
}
```

Figure 2.1: Standard C interface to BuDDy. In this mode both 'bdd' and 'BDD' can be used as BuDDy BDD types. The C interface requires the user to ensure garbage collection is handled correctly. This means calling 'bdd_addref' every time a new BDD is created, and 'bdd_delref' whenever a BDD is not in use anymore.

2.6 Dynamic Variable Reordering

Dynamic variable reordering can be done using the functions bdd_reorder(int method) and bdd_autoreorder(int method). Where the parameter method, for instance can be BDD_REORDER_WIN2ITE. The package must know how the BDD variables are related to each other, so the user must define blocks of BDD variables, using bdd_addvarblock(bdd var, int fixed). A block is a range of BDD variables that should be kept together. It may either be a simple contiguous sequence of variables or a sequence of other blocks with ranges inside their parents range. In this way all the blocks form a tree of ranges. Partially overlapping blocks are not allowed.

Example: Assume the block $v_0 ldots v_9$, is added as the first block and then the block $v_1 ldots v_8$. This yields the $v_0 ldots v_9$ block at the top, with the $v_1 ldots v_8$ block as a child. If now the block $v_1 ldots v_4$ was added, it would become a child of the $v_1 ldots v_8$ block, similarly the block $v_5 ldots v_8$ would be a child of the $v_1 ldots v_8$ block. If we add the variables v_1, v_2, v_3 and v_4 as single variable blocks we at last get tree showed in figure 2.4. If all variables should be added as single variable blocks then bdd_varblockall can be used instead of doing it manually.

The reordering algorithm is then to first reorder the top most blocks and there after descend into each block and reorder these recursively - unless the block is defined as a fixed block.

If the user want to control the swapping of variables himself, then the functions bdd_swapvar bdd_setvarorder may be used. But this is not possible in conjunction with the use of variable blocks and the bdd_swapvar is unfortunately quite slow since a full scan of all the nodes must be done both before and after the swap. Other reordering functions are bdd_autoreorder_times, bdd_reorder_verbose, bdd_sizeprobe_hook and bdd_reorder_hook.

```
#include <bdd.h>
main(void)
{
   bdd x,y,z;

   bdd_init(1000,100);
   bdd_setvarnum(5);

   x = bdd_ithvar(0);
   y = bdd_ithvar(1);
   z = x & y;

   cout << bddtable << z << endl;
   bdd_done();
}</pre>
```

Figure 2.2: C++ interface to BuDDy. In this mode 'bdd' is a C++ class that wraps a handler around the standard C interface, and the 'BDD' type referes to the standard C BDD type. The C++ interface handles all garbage collection, so no calls to 'bdd_addref' and 'bdd_delref' are needed.

2.7 Error Handling

If an error occurs then a check is done to see if there is any error handler defined and if so it is called with the error code of interest. The default error handler prints an error message on stderr and then aborts the program. A handler can also be defined by the user with a call to bdd_error_hook.

2.8 The C++ interface

Mostly this consists of a set of overloaded function wrappers that takes a bdd class and calls the appropriate C functions with the root number stored in the bdd class. The names of these wrappers are exactly the same as for the C functions. In addition to this a lot of the C++ operators like |&-|=| are overloaded in order to perform most of the bdd_apply() operations. These are listed together with bdd_apply. The rest are

Operator	Description	Return value
=	${\it assignment}$	
==	test	returns 1 if two BDDs are equal, otherwise 0
! =	test	returns 0 if two BDDs are equal, otherwise 1
bdd.id()	identity	returns the root number of the BDD

The default constructor for the bdd class initializes the bdds to the constant false value. Reference counting is totally automatic when the bdd class is used, here the constructors and destructors takes care of *all* reference counting! The C++ interface is also defined in bdd.h so nothing extra is needed to use it.

```
#include <bdd.h>
main()
{
   bdd v1, v3;
   bdd seta, setb;
   static int v[2] = \{1,3\};
   bdd_init(100,100);
   bdd setvarnum(5);
   v1 = bdd_ithvar(1);
   v3 = bdd_ithvar(3);
      /* One way */
   seta = bdd_addref( bdd_apply(v1,v3,bddop_and) );
   bdd_printtable(seta);
      /* Another way */
   setb = bdd_addref( bdd_makeset(v,2) );
   bdd_printtable(setb);
}
```

Figure 2.3: Two ways to create a variable set.

2.9 Finite Domain Blocks

Included in the BDD package is a set of functions for manipulating values of finite domains, like for example finite state machines. These functions are used to allocate blocks of BDD variables to represent integer values instead of only true and false.

New finite domain blocks are allocated using fdd_extdomain and BDDs representing integer values can be build using fdd_ithvar. The BDD representing identity between two sets of different domains can be build using fdd_equals. BDDs representing finite domain sets can be printed using fdd_printset and the overloaded C++ operator <<. Pairs for bdd_replace can be made using fdd_setpair and variable sets can be made using fdd_ithset and fdd_makeset. The finite domain block interface is defined for both C and C++. To use this interface you must include "fdd.h".

Encoding using FDDs are done with the Least Significant Bits first in the ordering (top of the BDD). Assume variables $V_0 \dots V_3$ are used to encode the value 12 - this would yield $V_0 = 0, V_1 = 0, V_2 = 1, V_3 = 1$.

An example program using the FDD interface can be found in the examples directory.

2.10 Boolean Vectors

Another interface layer for BuDDy implements boolean vectors for use with integer arithmetics. A boolean vector is simply an array of BDDs where each BDD represents one bit of an expression. To use this interface you must include "bvec.h". As an example, suppose we want to express the following assignment from an expression

```
x := y + 10
```

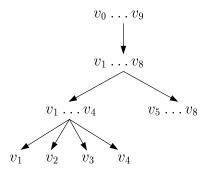


Figure 2.4: The variable tree for the variable blocks $v_0 \dots v_9$, $v_1 \dots v_8$, $v_1 \dots v_4$, $v_5 \dots v_8$, v_1 , v_2 , v_3 and v_4 .

what we do is to encode the variable y and the value 10 as boolean vectors y and v of a fixed length. Assume we use four bits with LSB to the right, then we get

$$y = \langle y_4, \dots, y_1 \rangle$$
$$v = \langle 1, 0, 1, 0 \rangle$$

where each y_i is the BDD variable used to encode the integer variable y. Now the result of the addition can be expressed as the vector $z = \langle z_4, \ldots, z_1 \rangle$ where each z_i is:

```
z_i = y_i \text{ xor } v_i \text{ xor } c_{i-1}
```

and the carry in c_i is

$$c_i = (y_i \text{ and } v_i) \text{ or } (c_{i-1} \text{ and } (y_i \text{ or } v_i)).$$

with $c_0 = 0$. What is left now is to assign the result to x. This is a conjunction of a biimplication of each element in the vectors, so the result is

$$R = \bigwedge_{i=1}^{4} x_i \Leftrightarrow z_i.$$

The above example could be carried out with the following C++ program that utilizes the FDD interface for printing the result.

```
#include "bvec.h"
```

```
main()
{
   int domain[2] = {16,16};

   bdd_init(100,100);
   fdd_extdomain(domain, 2);

   bvec y = bvec_varfdd(0);
   bvec v = bvec_con(4, 10);
   bvec z = bvec_add(y, v);

   bvec x = bvec_varfdd(1);
```

```
bdd result = bddtrue;
   for (int n=0; n < x.bitnum(); n++)
      result &= bdd_apply(x[n], z[n], bddop_biimp);
   cout << fddset << result << endl << endl;</pre>
}
The relational operators <,>,\leq,\geq,=,\neq can also be encoded. Assume we want to encode
x \leq y using the same variables as in the above example. This would be done as:
#include "bvec.h"
main()
{
   int domain[2] = \{16,16\};
   bdd_init(100,100);
   fdd_extdomain(domain, 2);
   bvec y = bvec_varfdd(1);
   bvec x = bvec_varfdd(0);
   bdd result = bvec_lte(x,y);
   cout << fddset << result << endl << endl;</pre>
}
Please note that all vectors that are returned from any of the bvec_xxx functions are
referenced counted by the system.
2.10.1 C++ Interface
The C++ interface defines the class
class bvec
{
 public:
   bvec(void);
   bvec(int bitnum);
   bvec(int bitnum, int val);
   bvec(const bvec &v);
   "bvec(void);
   void set(int i, const bdd &b);
   bdd operator[](int i) const;
   int bitnum(void) const;
```

int empty(void) const;

}

bvec operator=(const bvec &src);

The default constructor makes an empty vector with no elements, the integer constructor creates a vector with bitnum elements (all set to false) and the third constructor creates a vector with bitnum elements and assigns the integer value val to the vector. Reference counting is done automatically. The i'th element in the vector can be changed with set and read with operator[]. The number of bits can be found with bitnum and the method empty returns true if the vector is a NULL vector.

Efficiency Concerns

Getting the most out of any BDD package is not always easy. It requires some knowledge about the optimal order of the BDD variables and it also helps if you have some knowledge of the internals of the package.

First of all — a good initial variable order is a must. Using the automatic reordering methods may be an easy solution, but without a good initial order it may also be a waste of time.

Second — memory is speed. If you allocate as much memory as possible from the very beginning, then BuDDy does not have to waste time trying to allocate more whenever it is needed. So if you really want speed then bdd_init should be called with as many nodes as possible. This does unfortunately have the side effect that variable reordering becomes extremely slow since it has to reorder an enormous amount of nodes the first time it is triggered.

Third—the operator caches should be as big as possible. Use the function bdd_setcacheratio to make sure the size of these is increased whenever more nodes are allocated. Please note that BuDDy uses a fixed number of elements for these caches as default. You must call bdd_setcacheratio to change this. I have found a cache ratio of 1:64 fitting for BDDs of more than one million nodes (the solitare example). This may be a bit overkill, but it works.

Fourth — BuDDy allocates by default a maximum of 50000 nodes (1Mb RAM) every time it resizes the node table. If your problem needs millions of nodes, then this is way too small a number. Use bdd_setmaxincrease to increase this number. In the solitare example something like 5000000 nodes seems more reasonable.

Fifth — by default, BuDDy increases the node table whenever there is less than 20% nodes free. By increasing this value you can make BuDDy go faster and use more memory or vice versa. You can change the value with bdd_setminfreenodes.

So, to sum it up: if you want speed, then allocate as many nodes as possible, use small cache ratios and set maxincrease. If you need memory, then allocate a small number of nodes from the beginning, use a fixed size cache, do not change maxincrease and lower minfreenodes.

Some Implementation details

- Negated pointers are not used.
- All nodes are stored in one big contiguous array which is also used as the hash table for finding identical nodes.
- The hash function used to find identical nodes from the triple (level, low, high) spreads all nodes evenly in the table. This means the average length of a hash chain is at most 1.
- Each node in the node table contains a reference count, the level of the variable (this is its position in the current variable order), the high and low part, a hash index used to find the first node in a hash chain and a next index used to link the hash chains. Each node fits into 20 bytes of memory. Other packages uses only 16 bytes for each node but in addition to this they must keep separate tables with hash table entries. The effect of this is that the total memory consumption is 20 bytes for each node on average.
- Reference counting are done on the externally referenced nodes only.
- The ANSI-C bdd type is an integer number referring to an index in the node table. In C++ it is a class.
- New nodes are created by doubling (or just extending) the node table, not by adding new blocks of nodes.
- Garbage collection recursively marks all nodes reachable from the externally referenced nodes before dead nodes are removed.
- Reordering interrupts the current BDD operation and restarts it again afterwards.
- Reordering changes the hash function to one where all nodes of a specific level is placed in one continuous block and updates the reference count field to include all recursive dependencies. After reordering the package returns to the normal hash function.

Reference

Boolean vector	rs
bvec	a boolean vector
bvec_add	builds a boolean vector for addition
bvec_addref	increase reference count of a boolean vector
bvec_coerce	adjust the size of a boolean vector
bvec_con	build a boolean vector representing an integer value
bvec_copy	create a copy of a bvec
bvec_delref	decrease the reference count of a boolean vector
bvec_div	builds a boolean vector for division
bvec_divfixed	builds a boolean vector for division by a constant
bvec_equ	calculates the truth value of $x = y$
bvec_false	build a vector of constant false BDDs
bvec_free	frees all memory used by a boolean vector
bvec_gte	calculates the truth value of $x \geq y$
bvec_gth	calculates the truth value of $x > y$
bvec_isconst	test a vector for constant true/false BDDs
bvec_ite	calculates the if-then-else operator for a boolean vector
bvec_lte	calculates the truth value of $x \leq y$
bvec_lth	calculates the truth value of $x < y$
bvec_map1	map a function onto a boolean vector
bvec_map2	map a function onto a boolean vector
bvec_map3	map a function onto a boolean vector
bvec_mul	builds a boolean vector for multiplication
bvec_mulfixed	builds a boolean vector for multiplication with a constant
bvec_neq	calculates the truth value of $x \neq y$
bvec_shl	shift left operation (symbolic)
bvec_shlfixed	shift left operation (fixed number of bits)
bvec_shr	shift right operation (symbolic)
bvec_shrfixed	shift right operation
bvec_sub	builds a boolean vector for subtraction
bvec_true	build a vector of constant true BDDs
bvec_val	calculate the integer value represented by a boolean vector
bvec_var	build a boolean vector with BDD variables

bvec_varfdd	build a boolean vector from a FDD variable block
bvec_varvec	build a boolean vector with the variables passed in an array
Finite domain varia	_
fdd_clearall	clear all allocated FDD blocks
fdd_domain	bDD encoding of the domain of a FDD variable
fdd_domainnum	number of defined finite domain blocks
fdd_domainsize	real size of a finite domain block
fdd_equals	returns a BDD setting two FD. blocks equal
fdd_extdomain	adds another set of finite domain blocks
fdd_file_hook	specifies a printing callback handler
fdd_intaddvarblock	adds a new variable block for reordering
fdd_ithset	the variable set for the i'th finite domain block
fdd_ithvar	the BDD for the i'th FDD set to a specific value
fdd_makeset	creates a variable set for N finite domain blocks
fdd_overlapdomain	combine two FDD blocks into one
fdd_printset	prints a BDD for a finite domain block
fdd_fprintset	printed a DDD for a finite domain block
fdd_scanallvar	finds one satisfying value of all FDD variables
fdd_scanset	scans a variable set
fdd scanvar	finds one satisfying value of a FDD variable
fdd_setpair	defines a pair for two finite domain blocks
fdd_setpairs	defines N pairs for finite domain blocks
fdd_strm_hook	specifies a printing callback handler
fdd_varnum	binary size of a finite domain block
fdd_vars	all BDD variables associated with a finite domain block
File input/output	an BBB variables associated with a limite deficial stock
bdd_load	loads a BDD from a file
bdd_fnload	
bdd_printall	prints all used entries in the node table
bdd_fprintall	r
bdd_printdot	prints a description of a BDD in DOT format
bdd_fprintdot	
bdd_printset	prints the set of truth assignments specified by a BDD
bdd_fprintset	
bdd_printtable	prints the node table entries used by a BDD
bdd_fprinttable	·
bdd_save	saves a BDD to a file
bdd_fnsave	
operator<<	c++ output operator for BDDs
Information on BDI	
bdd_anodecount	counts the number of shared nodes in an array of BDDs
bdd_high	gets the true branch of a bdd
bdd_low	gets the false branch of a bdd
bdd_nodecount	counts the number of nodes used for a BDD
bdd_pathcount	count the number of paths leading to the true terminal
<u> </u>	·

h d d	leadaulates the number of satisfying regionly assignments
bdd_satcount	calculates the number of satisfying variable assignments
bdd_setcountset	
bdd_satcountln bdd_setcountlnset	calculates the log. number of satisfying variable assignments
	notes and the control of a DDD
bdd_support	returns the variable support of a BDD
bdd_var	gets the variable labeling the bdd
bdd_varprofile	returns a variable profile
	ons and data structures
bddCacheStat	status information about cache usage
bddGbcStat	status information about garbage collections
bddStat	status information about the bdd package
bdd_addref	increases the reference count on a node
bdd_cachestats	fetch cache access usage
bdd_clear_error	clears an error condition in the kernel
bdd_delref	decreases the reference count on a node
bdd_done	resets the bdd package
bdd_error_hook	set a handler for error conditions
bdd_errstring	converts an error code to a string
bdd_extvarnum	add extra BDD variables
bdd_false	returns the constant false bdd
bdd_file_hook	specifies a printing callback handler
bdd_freepair	frees a table of pairs
bdd_gbc_hook	set a handler for garbage collections
bdd_getallocnum	get the number of allocated nodes
bdd_getnodenum	get the number of active nodes in use
bdd_init	initializes the BDD package
bdd_isrunning	test whether the package is started or not
bdd_ithvar	returns a bdd representing the I'th variable
bdd_makeset	builds a BDD variable set from an integer array
bdd_newpair	creates an empty variable pair table
bdd_nithvar	returns a bdd representing the negation of the I'th variable
bdd_printstat	print cache statistics
bdd_fprintstat	
bdd_resetpair	clear all variable pairs
bdd_resize_hook	set a handler for nodetable resizes
bdd_scanset	returns an integer representation of a variable set
bdd_setcacheratio	sets the cache ratio for the operator caches
bdd_setmaxincrease	set max. number of nodes used to increase node table
bdd_setmaxnodenum	set the maximum available number of bdd nodes
bdd_setminfreenodes	set min. no. of nodes to be reclaimed after GBC.
bdd_setpair	set one variable pair
bdd_setbddpair	
bdd_setpairs	defines a whole set of pairs
bdd_setbddpairs	
bdd_setvarnum	set the number of used bdd variables
	ı

bdd_stats	returns some status information about the bdd package	
bdd_strm_hook	specifies a printing callback handler	
bdd_true	returns the constant true bdd	
bdd_varnum	returns the number of defined variables	
bdd_versionnum	returns the version number of the bdd package	
bdd_versionstr	returns a text string with version information	
bddfalse	the constant false bdd	
bddtrue	the constant true bdd	
BDD operators		
bdd_allsat	finds all satisfying variable assignments	
bdd_and	the logical 'and' of two BDDs	
bdd_appall	apply operation and universal quantification	
bdd_appex	apply operation and existential quantification	
bdd_apply	basic bdd operations	
bdd_appuni	apply operation and unique quantification	
bdd_biimp	the logical 'bi-implication' between two BDDs	
bdd_buildcube	build a cube from an array of variables	
bdd_ibuildcube		
bdd_compose	functional composition	
bdd_constrain	generalized cofactor	
bdd_exist	existential quantification of variables	
bdd_forall	universal quantification of variables	
bdd_fullsatone	finds one satisfying variable assignment	
bdd_imp	the logical 'implication' between two BDDs	
bdd_ite	if-then-else operator	
bdd_not	negates a bdd	
bdd_or	the logical 'or' of two BDDs	
bdd_relprod	relational product	
bdd_replace	replaces variables with other variables	
bdd_restrict	restric a set of variables to constant values	
bdd_satone	finds one satisfying variable assignment	
bdd_satoneset	finds one satisfying variable assignment	
bdd_simplify	coudert and Madre's restrict function	
bdd_unique	unique quantification of variables	
bdd_veccompose	simultaneous functional composition	
bdd_xor	the logical 'xor' of two BDDs	
Variable reordering		
bdd_addvarblock	adds a new variable block for reordering	
bdd_intaddvarblock		
bdd_autoreorder	enables automatic reordering	
bdd_autoreorder_times		
bdd_blockfile_hook	specifies a printing callback handler	
bdd_clrvarblocks	clears all variable blocks	
bdd_disable_reorder	disable automatic reordering	
bdd_enable_reorder	enables automatic reordering	

bdd_getreorder_method	fetch the current reorder method
bdd_getreorder_times	fetch the current number of allowed reorderings
bdd_level2var	fetch the variable number of a specific level
bdd_printorder	prints the current order
bdd_reorder	start dynamic reordering
bdd_reorder_gain	calculate the gain in size after a reordering
bdd_reorder_hook	sets a handler for automatic reorderings
bdd_reorder_probe	define a handler for minimization of BDDs
bdd_reorder_verbose	enables verbose information about reorderings
bdd_setvarorder	set a specific variable order
bdd_swapvar	swap two BDD variables
bdd_var2level	fetch the level of a specific BDD variable
bdd_varblockall	add a variable block for all variables

bddCacheStat - Status information about cache usage

```
typedef struct s_bddCacheStat
{
   long unsigned int uniqueAccess;
   long unsigned int uniqueChain;
   long unsigned int uniqueHit;
   long unsigned int uniqueMiss;
   long unsigned int opHit;
   long unsigned int opMiss;
   long unsigned int swapCount;
} bddCacheStat;
```

Description

The fields are

\mathbf{Name}	Number of
uniqueAccess	accesses to the unique node table
uniqueChain	iterations through the cache chains in the unique node table
${ m unique Hit}$	entries actually found in the the unique node table
uniqueMiss	entries not found in the the unique node table
opHit	entries found in the operator caches
opMiss	entries not found in the operator caches
swapCount	number of variable swaps in reordering

See also

bdd_cachestats

bddGbcStat - Status information about garbage collections

```
typedef struct s_bddGbcStat
{
   int nodes;
   int freenodes;
   long time;
   long sumtime;
   int num;
} bddGbcStat;
```

Description

The fields are

nodes Total number of allocated nodes in the nodetable

freenodes Number of free nodes in the nodetable
time Time used for garbage collection this time
sumtime Total time used for garbage collection

num number of garbage collections done until now

See also

 bdd_gbc_hook

bddStat - Status information about the bdd package

```
typedef struct s_bddStat
{
   long int produced;
   int nodenum;
   int maxnodenum;
   int freenodes;
   int minfreenodes;
   int varnum;
   int cachesize;
   int gbcnum;
}
```

Description

The fields are

producedtotal number of new nodes ever producednodenumcurrently allocated number of bdd nodesmaxnodenumuser defined maximum number of bdd nodes

freenodes number of currently free nodes

minfreenodes minimum number of nodes that should be left after a

garbage collection.

varnum number of defined bdd variables

cachesize number of entries in the internal caches

gbcnum number of garbage collections done until now

See also

 bdd_stats

bdd_addref – increases the reference count on a node

```
BDD bdd_addref(BDD r)
```

Description

Reference counting is done on externally referenced nodes only and the count for a specific node \mathbf{r} can and must be increased using this function to avoid loosing the node in the next garbage collection.

Return value

The BDD node r.

See also

bdd_delref

bdd_addvarblock – adds a new variable block for reordering

```
int bdd_addvarblock(BDD var, int fixed)
int bdd_intaddvarblock(int first, int last, int fixed)
```

Description

Creates a new variable block with the variables in the variable set var. The variables in var must be contiguous. In the second form the argument first is the first variable included in the block and last is the last variable included in the block. This order does not depend on current variable order.

The variable blocks are ordered as a tree, with the largest ranges at top and the smallest at the bottom. Example: Assume the block 0-9 is added as the first block and then the block 0-6. This yields the 0-9 block at the top, with the 0-6 block as a child. If now the block 2-4 was added, it would become a child of the 0-6 block. A block of 0-8 would be a child of the 0-9 block and have the 0-6 block as a child. Partially overlapping blocks are not allowed.

The fixed parameter sets the block to be fixed (no reordering of its child blocks is allowed) or free, using the constants BDD_REORDER_FIXED and BDD_REORDER_FREE. Reordering is always done on the top most blocks first and then recursively downwards.

The return value is an integer that can be used to identify the block later on - with for example bdd_blockfile_hook. The values returned will be in the sequence 0, 1, 2, 3,

Return value

A non-negative identifier on success, otherwise a negative error code.

See also

bdd_varblockall, fdd_intaddvarblock, bdd_clrvarblocks

```
BDD bdd_satone(BDD r, bddallsathandler handler)
```

Description

Iterates through all legal variable assignments (those that make the BDD come true) for the bdd r and calls the callback handler handler for each of them. The array passed to handler contains one entry for each of the globaly defined variables. Each entry is either 0 if the variable is false, 1 if it is true, and -1 if it is a don't care.

The following is an example of a callback handler that prints 'X' for don't cares, '0' for zero, and '1' for one:

```
void allsatPrintHandler(char* varset, int size)
{
  for (int v=0; v<size ; ++v)
  {
    cout << (varset[v] < 0 ? 'X' : (char)('0' + varset[v]));
  }
  cout << endl;
}</pre>
```

The handler can be used like this: bdd_allsat(r, allsatPrintHandler);

See also

bdd_satone bdd_satoneset, bdd_fullsatone, bdd_satcount, bdd_satcountln

bdd_and – The logical 'and' of two BDDs

```
BDD bdd_and(BDD 1, BDD r)
```

Description

This a wrapper that calls bdd_apply(1,r,bddop_and).

Return value

The logical 'and' of 1 and r.

See also

bdd_apply, bdd_or, bdd_xor

bdd_anodecount – counts the number of shared nodes in an array of BDDs

int bdd_anodecount(BDD *r, int num)

Description

Traverses all of the BDDs in **r** and counts all distinct nodes that are used in the BDDs-if a node is used in more than one BDD then it only counts once. The **num** parameter holds the size of the array.

Return value

The number of nodes

See also

bdd_nodecount

bdd_appall – apply operation and universal quantification

BDD bdd_appall(BDD left, BDD right, int opr, BDD var)

Description

Applies the binary operator opr to the arguments left and right and then performs an universal quantification of the variables from the variable set var. This is done in a bottom up manner such that both the apply and quantification is done on the lower nodes before stepping up to the higher nodes. This makes the bdd_appall function much more efficient than an apply operation followed by a quantification.

Return value

The result of the operation.

See also

bdd_appex, bdd_appuni, bdd_apply, bdd_exist, bdd_forall, bdd_unique, bdd_makeset

bdd_appex – apply operation and existential quantification

BDD bdd_appex(BDD left, BDD right, int opr, BDD var)

Description

Applies the binary operator opr to the arguments left and right and then performs an existential quantification of the variables from the variable set var. This is done in a bottom up manner such that both the apply and quantification is done on the lower nodes before stepping up to the higher nodes. This makes the bdd_appex function much more efficient than an apply operation followed by a quantification. If the operator is a conjunction then this is similar to the relational product of the two BDDs.

Return value

The result of the operation.

See also

bdd_appall, bdd_appuni, bdd_apply, bdd_exist, bdd_forall, bdd_unique, bdd_makeset

bdd_apply – basic bdd operations

BDD bdd_apply(BDD left, BDD right, int opr)

Description

The bdd_apply function performs all of the basic bdd operations with two operands, such as AND, OR etc. The left argument is the left bdd operand and right is the right operand. The opr argument is the requested operation and must be one of the following

Identifier	Description	Truth table	C++ opr
bddop_and	logical and $(A \wedge B)$	[0,0,0,1]	&
bddop_xor	logical xor $(A \oplus B)$	[0,1,1,0]	^
bddop_or	logical or $(A \vee B)$	[0, 1, 1, 1]	1
bddop_nand	logical not-and	[1,1,1,0]	
bddop_nor	logical not-or	[1,0,0,0]	
$bddop_imp$	implication $(A \Rightarrow B)$	[1, 1, 0, 1]	>>
bddop_biimp	bi-implication $(A \Leftrightarrow B)$	[1,0,0,1]	
bddop_diff	set difference $(A \setminus B)$	[0,0,1,0]	_
bddop_less	less than $(A < B)$	[0,1,0,0]	<
bddop_invimp	reverse implication $(A \Leftarrow B)$	[1,0,1,1]	<<

Return value

The result of the operation.

See also

bdd_ite

bdd_appuni - apply operation and unique quantification

BDD bdd_appuni(BDD left, BDD right, int opr, BDD var)

Description

Applies the binary operator opr to the arguments left and right and then performs a unique quantification of the variables from the variable set var. This is done in a bottom up manner such that both the apply and quantification is done on the lower nodes before stepping up to the higher nodes. This makes the bdd_appuni function much more efficient than an apply operation followed by a quantification.

Return value

The result of the operation.

See also

bdd_appex, bdd_appall, bdd_apply, bdd_exist, bdd_unique, bdd_forall, bdd_makeset

bdd_autoreorder – enables automatic reordering

```
int bdd_autoreorder(int method)
int bdd_autoreorder_times(int method, int num)
```

Description

Enables automatic reordering using method as the reordering method. If method is BDD_REORDER_NONE then automatic reordering is disabled. Automatic reordering is done every time the number of active nodes in the node table has been doubled and works by interrupting the current BDD operation, doing the reordering and the retrying the operation.

In the second form the argument num specifies the allowed number of reorderings. So if for example a "one shot" reordering is needed, then the num argument would be set to one.

Values for method can be found under bdd_reorder.

Return value

Returns the old value of method

See also

bdd_reorder

bdd_biimp – The logical 'bi-implication' between two BDDs

```
BDD bdd_biimp(BDD 1, BDD r)
```

Description

This a wrapper that calls bdd_apply(1,r,bddop_biimp).

Return value

The logical 'bi-implication' of 1 and \mathbf{r} ($l \Leftrightarrow r$).

See also

bdd_apply, bdd_imp

bddfilehandler bdd_blockfile_hook(bddfilehandler handler)

Description

A printing callback handler is used to convert the variable block identifiers into something readable by the end user. Use bdd_blockfile_hook to pass a handler to BuDDy. A typical handler could look like this:

```
void printhandler(FILE *o, int block)
{
   extern char **blocknames;
   fprintf(o, "%s", blocknames[block]);
}
```

The handler is then called from bdd_printorder and bdd_reorder (depending on the verbose level) with the block numbers returned by bdd_addvarblock as arguments. No default handler is supplied. The argument handler may be NULL if no handler is needed.

Return value

The old handler

See also

bdd_printorder

bdd_buildcube – build a cube from an array of variables

```
BDD bdd_buildcube(int value, int width, BDD *var)
BDD bdd_ibuildcube(int value, int width, int *var)
```

Description

This function builds a cube from the variables in var. It does so by interpreting the width low order bits of value as a bit mask—a set bit indicates that the variable should be added in it's positive form, and a cleared bit the opposite. The most significant bits are encoded with the first variables in var. Consider as an example the call bdd_buildcube(0xB, 4, var). This corresponds to the expression: $var[0] \land \neg var[1] \land var[2] \land var[3]$. The first version of the function takes an array of BDDs, whereas the second takes an array of variable numbers as used in bdd_ithvar.

Return value

The resulting cube

See also

bdd_ithvar, fdd_ithvar

bdd_cachestats – Fetch cache access usage

void bdd_cachestats(bddCacheStat *s)

Description

Fetches cache usage information and stores it in s. The fields of s can be found in the documentaion for bddCacheStat. This function may or may not be compiled into the BuDDy package - depending on the setup at compile time of BuDDy.

See also

bddCacheStat, bdd_printstat

bdd_clear_error – clears an error condition in the kernel

void bdd_clear_error(void)

Description

The BuDDy kernel may at some point run out of new ROBDD nodes if a maximum limit is set with bdd_setmaxnodenum. In this case the current error handler is called and an internal error flag is set. Further calls to BuDDy will always return bddfalse. From here BuDDy must either be restarted or bdd_clear_error may be called after action is taken to let BuDDy continue. This may not be especially usefull since the default error handler exits the program - other needs may of course exist.

See also

bdd_error_hook, bdd_setmaxnodenum

bdd_clrvarblocks – clears all variable blocks

void bdd_clrvarblocks(void)

Description

Clears all the variable blocks that has been defined by calls to bdd_addvarblock.

See also

 $bdd_addvarblock$

bdd_compose – functional composition

BDD bdd_compose(BDD f, BDD g, int var)

Description

Substitutes the variable var with the BDD g in the BDD f: result = f[g/var].

Return value

The composed BDD

See also

bdd_veccompose, bdd_replace, bdd_restrict

bdd_constrain – generalized cofactor

BDD bdd_constrain(BDD f, BDD c)

Description

Computes the generalized cofactor of f with respect to c.

Return value

The constrained BDD

See also

bdd_restrict, bdd_simplify



BDD bdd_delref(BDD r)

Description

Reference counting is done on externally referenced nodes only and the count for a specific node \mathbf{r} can and must be decreased using this function to make it possible to reclaim the node in the next garbage collection.

Return value

The BDD node r.

See also

bdd_addref

bdd_disable_reorder – Disable automatic reordering

void bdd_disable_reorder(void)

Description

Disables automatic reordering until bdd_enable_reorder is called. Reordering is enabled by default as soon as any variable blocks have been defined.

See also

bdd_enable_reorder

bdd_done - resets the bdd package

void bdd_done(void)

Description

This function frees all memory used by the bdd package and resets the package to it's initial state.

See also

bdd_init

bdd_enable_reorder – Enables automatic reordering

```
void bdd_enable_reorder(void)
```

Description

Re-enables reordering after a call to bdd_disable_reorder.

See also

bdd_disable_reorder

bdd_error_hook – set a handler for error conditions

bddinthandler bdd_error_hook(bddinthandler handler)

Description

Whenever an error occurs in the bdd package a test is done to see if an error handler is supplied by the user and if such exists then it will be called with an error code in the variable errcode. The handler may then print any usefull information and return or exit afterwards.

This function sets the handler to be handler. If a NULL argument is supplied then no calls are made when an error occurs. Possible error codes are found in bdd.h. The default handler is bdd_default_errhandler which will use exit() to terminate the program.

Any handler should be defined like this:

```
void my_error_handler(int errcode)
{
    ...
}
```

Return value

The previous handler

See also

bdd_errstring

bdd_errstring – converts an error code to a string

const char *bdd_errstring(int errorcode)

Description

Converts a negative error code errorcode to a descriptive string that can be used for error handling.

Return value

An error description string if e is known, otherwise NULL.

See also

bdd_err_hook

bdd_exist – existential quantification of variables

BDD bdd_exist(BDD r, BDD var)

Description

Removes all occurences in r of variables in the set var by existential quantification.

Return value

The quantified BDD.

See also

bdd_forall, bdd_unique, bdd_makeset

bdd_extvarnum – add extra BDD variables

int bdd_extvarnum(int num)

Description

Extends the current number of allocated BDD variables with num extra variables.

Return value

The old number of allocated variables or a negative error code.

See also

bdd_setvarnum, bdd_ithvar, bdd_nithvar

bdd_false – returns the constant false bdd

```
BDD bdd_false(void)
```

Description

This function returns the constant false bdd and can freely be used together with the bddtrue and bddfalse constants.

Return value

The constant false bdd

See also

bdd_true, bddtrue, bddfalse

bdd_file_hook – Specifies a printing callback handler

bddfilehandler bdd_file_hook(bddfilehandler handler)

Description

A printing callback handler for use with BDDs is used to convert the BDD variable number into something readable by the end user. Typically the handler will print a string name instead of the number. A handler could look like this:

```
void printhandler(FILE *o, int var)
{
   extern char **names;
   fprintf(o, "%s", names[var]);
}
```

The handler can then be passed to BuDDy like this: bdd_file_hook(printhandler).

No default handler is supplied. The argument handler may be NULL if no handler is needed.

Return value

The old handler

See also

bdd_printset, bdd_strm_hook, fdd_file_hook

bdd_forall – universal quantification of variables

BDD bdd_forall(BDD r, BDD var)

Description

Removes all occurences in r of variables in the set var by universal quantification.

Return value

The quantified BDD.

See also

bdd_exist, bdd_unique, bdd_makeset

bdd_freepair - frees a table of pairs

void bdd_freepair(bddPair *pair)

Description

Frees the table of pairs pair that has been allocated by a call to bdd_newpair.

See also

bdd_replace, bdd_newpair, bdd_setpair, bdd_resetpair

bdd_fullsatone – finds one satisfying variable assignment

BDD bdd_fullsatone(BDD r)

Description

Finds a BDD with exactly one variable at all levels. This BDD implies \mathbf{r} and is not false unless \mathbf{r} is false.

Return value

The result of the operation.

See also

bdd_allsat bdd_satone, bdd_satoneset, bdd_satcount, bdd_satcountln

bdd_gbc_hook – set a handler for garbage collections

bddgbchandler bdd_gbc_hook(bddgbchandler handler)

Description

Whenever a garbage collection is required, a test is done to see if a handler for this event is supplied by the user and if such exists then it is called, both before and after the garbage collection takes places. This is indicated by an integer flag **pre** passed to the handler, which will be one before garbage collection and zero after garbage collection.

This function sets the handler to be handler. If a NULL argument is supplied then no calls are made when a garbage collection takes place. The argument pre indicates pre vs. post garbage collection and the argument stat contains information about the garbage collection. The default handler is bdd_default_gbchandler.

Any handler should be defined like this:

```
void my_gbc_handler(int pre, bddGbcStat *stat)
{
    ...
}
```

Return value

The previous handler

See also

bdd_resize_hook, bdd_reorder_hook

bdd_getallocnum – get the number of allocated nodes

int bdd_getallocnum(void)

Description

Returns the number of nodes currently allocated. This includes both dead and active nodes.

Return value

The number of nodes.

See also

bdd_getnodenum, bdd_setmaxnodenum

bdd_getnodenum – get the number of active nodes in use

int bdd_getnodenum(void)

Description

Returns the number of nodes in the nodetable that are currently in use. Note that dead nodes that have not been reclaimed yet by a garbage collection are counted as active.

Return value

The number of nodes.

See also

bdd_getallocnum, bdd_setmaxnodenum

bdd_getreorder_method – Fetch the current reorder method

int bdd_getreorder_method(void)

Description

Returns the current reorder method as defined by bdd_autoreorder.

See also

bdd_reorder, bdd_getreorder_times

bdd_getreorder_times – Fetch the current number of allowed reorderings

int bdd_getreorder_times(void)

Description

Returns the current number of allowed reorderings left. This value can be defined by bdd_autoreorder_times.

See also

bdd_reorder_times, bdd_getreorder_method

bdd_high – gets the true branch of a bdd

BDD bdd_high(BDD r)

Description

Gets the true branch of the bdd r.

Return value

The bdd of the true branch

See also

 bdd_low

bdd_imp – The logical 'implication' between two BDDs

BDD bdd_imp(BDD 1, BDD r)

Description

This a wrapper that calls bdd_apply(1,r,bddop_imp).

Return value

The logical 'implication' of 1 and $r(l \Rightarrow r)$.

See also

bdd_apply, bdd_biimp

bdd_init - initializes the BDD package

int bdd_init(int nodesize, int cachesize)

Description

This function initiates the bdd package and *must* be called before any bdd operations are done. The argument nodesize is the initial number of nodes in the nodetable and cachesize is the fixed size of the internal caches. Typical values for nodesize are 10000 nodes for small test examples and up to 1000000 nodes for large examples. A cache size of 10000 seems to work good even for large examples, but lesser values should do it for smaller examples.

The number of cache entries can also be set to depend on the size of the nodetable using a call to bdd_setcacheratio.

The initial number of nodes is not critical for any bdd operation as the table will be resized whenever there are to few nodes left after a garbage collection. But it does have some impact on the efficiency of the operations.

Return value

If no errors occur then 0 is returned, otherwise a negative error code.

See also

bdd_done, bdd_resize_hook

bdd_isrunning – test whether the package is started or not

void bdd_isrunning(void)

Description

This function tests the internal state of the package and returns a status.

Return value

1 (true) if the package has been started, otherwise 0.

See also

bdd_init, bdd_done

bdd_ite – if-then-else operator

BDD bdd_ite(BDD f, BDD g, BDD h)

Description

Calculates the BDD for the expression $(f \wedge g) \vee (\neg f \wedge h)$ more efficiently than doing the three operations separately. bdd_ite can also be used for conjunction, disjunction and any other boolean operator, but is not as efficient for the binary and unary operations.

Return value

The BDD for $(f \wedge g) \vee (\neg f \wedge h)$

See also

bdd_apply

bdd_ithvar – returns a bdd representing the I'th variable

BDD bdd_ithvar(int var)

Description

This function is used to get a bdd representing the I'th variable (one node with the childs true and false). The requested variable must be in the range define by bdd_setvarnum starting with 0 being the first. For ease of use then the bdd returned from bdd_ithvar does not have to be referenced counted with a call to bdd_addref. The initial variable order is defined by the the index var that also defines the position in the variable order – variables with lower indecies are before those with higher indecies.

Return value

The I'th variable on succes, otherwise the constant false bdd

See also

bdd_setvarnum, bdd_nithvar, bddtrue, bddfalse

bdd_level2var – Fetch the variable number of a specific level

int bdd level2var(int level)

Description

Returns the variable placed at position level in the current variable order.

See also

bdd_reorder, bdd_var2level

bdd_load – loads a BDD from a file

```
int bdd_fnload(char *fname, BDD *r)
int bdd_load(FILE *ifile, BDD *r)
```

Description

Loads a BDD from a file into the BDD pointed to by r. The file can either be the file ifile which must be opened for reading or the file named fname which will be opened automatically for reading.

The input file format consists of integers arranged in the following manner. First the number of nodes N used by the BDD and then the number of variables V allocated and the variable ordering in use at the time the BDD was saved. If N and V are both zero then the BDD is either the constant true or false BDD, indicated by a 1 or a 0 as the next integer.

In any other case the next N sets of 4 integers will describe the nodes used by the BDD. Each set consists of first the node number, then the variable number and then the low and high nodes.

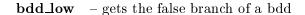
The nodes *must* be saved in a order such that any low or high node must be defined before it is mentioned.

Return value

Zero on succes, otherwise an error code from bdd.h.

See also

bdd_save



BDD bdd_low(BDD r)

Description

Gets the false branch of the bdd r.

Return value

The bdd of the false branch

See also

bdd_high

bdd_makeset - builds a BDD variable set from an integer array

BDD bdd_makeset(int *v, int n)

Description

Reads a set of variable numbers from the integer array v which must hold exactly n integers and then builds a BDD representing the variable set.

The BDD variable set is represented as the conjunction of all the variables in their positive form and may just as well be made that way by the user. The user should keep a reference to the returned BDD instead of building it every time the set is needed.

Return value

A BDD variable set.

See also

bdd_scanset

bdd_newpair - creates an empty variable pair table

bddPair *bdd_newpair(void)

Description

Variable pairs of the type bddPair are used in bdd_replace to define which variables to replace with other variables. This function allocates such an empty table. The table can be freed by a call to bdd_freepair.

Return value

Returns a new table of pairs.

See also

bdd_freepair, bdd_replace, bdd_setpair, bdd_setpairs

bdd_nithvar – returns a bdd representing the negation of the I'th variable

BDD bdd_nithvar(int var)

Description

This function is used to get a bdd representing the negation of the I'th variable (one node with the childs false and true). The requested variable must be in the range define by bdd_setvarnum starting with 0 being the first. For ease of use then the bdd returned from bdd_nithvar does not have to be referenced counted with a call to bdd_addref.

Return value

The negated I'th variable on succes, otherwise the constant false bdd

See also

bdd_setvarnum, bdd_ithvar, bddtrue, bddfalse

bdd_nodecount – counts the number of nodes used for a BDD

int bdd_nodecount(BDD r)

Description

Traverses the BDD and counts all distinct nodes that are used for the BDD.

Return value

The number of nodes.

See also

bdd_pathcount, bdd_satcount, bdd_anodecount

bdd_not – negates a bdd

BDD bdd_not(BDD r)

Description

Negates the BDD r by exchanging all references to the zero-terminal with references to the one-terminal and vice versa.

Return value

The negated bdd.

bdd_or – The logical 'or' of two BDDs

BDD bdd_or(BDD 1, BDD r)

Description

This a wrapper that calls bdd_apply(1,r,bddop_or).

Return value

The logical 'or' of 1 and r.

See also

bdd_apply, bdd_xor, bdd_and

bdd_pathcount – count the number of paths leading to the true terminal

double bdd_pathcount(BDD r)

Description

Counts the number of paths from the root node r leading to the terminal true node.

Return value

The number of paths

See also

bdd_nodecount, bdd_satcount

bdd_printall - prints all used entries in the node table

```
void bdd_printall(void)
void bdd_fprintall(FILE* ofile)
```

Description

Prints to either stdout or the file ofile all the used entries in the main node table. The format is:

[Nodenum] Var/level Low High

Where Nodenum is the position in the node table and level is the position in the current variable order.

See also

bdd_printtable, bdd_printset, bdd_printdot

bdd_printdot – prints a description of a BDD in DOT format

```
void bdd_printdot(BDD r)
int bdd_fnprintdot(char* fname, BDD r)
void bdd_fprintdot(FILE* ofile, BDD r)
```

Description

Prints a BDD in a format suitable for use with the graph drawing program DOT to either stdout, a designated file ofile or the file named by fname. In the last case the file will be opened for writing, any previous contents destroyed and then closed again.

See also

bdd_printall, bdd_printable, bdd_printset

bdd_printorder – prints the current order

```
void bdd_printorder(void)
bdd_fprint_order(FILE *f)
```

Description

Prints an indented list of the variable blocks, showing the top most blocks to the left and the lower blocks to the right. Example:

This shows 5 variable blocks. The first one added is block zero, which is on the same level as block one. These two blocks are then sub-blocks of block two and block two is on the same level as block three and four. The numbers are the identifiers returned from bdd_addvarblock. The block levels depends on the variables included in the blocks.

See also

bdd_reorder, bdd_addvarblock

bdd_printset – prints the set of truth assignments specified by a BDD

```
bdd_printset(BDD r)
bdd_fprintset(FILE* ofile, BDD r)
```

Description

Prints all the truth assignments for \mathbf{r} that would yield it true. The format is:

```
 < x_{1,1}: c_{1,1}, \dots, x_{1,n_1}: c_{1,n_1} > \\ < x_{2,1}: c_{2,1}, \dots, x_{2,n_2}: c_{2,n_2} > \\ \dots \\ < x_{N,1}: c_{N,1}, \dots, x_{N,n_3}: c_{N,n_3} >
```

Where the x's are variable numbers (and the position in the current order) and the c's are the possible assignments to these. Each set of brackets designates one possible assignment to the set of variables that make up the BDD. All variables not shown are don't cares. It is possible to specify a callback handler for printing of the variables using bdd_file_hook or bdd_strm_hook.

See also

bdd_printall, bdd_printtable, bdd_printdot, bdd_file_hook, bdd_strm_hook

bdd_printstat – print cache statistics

```
void bdd_printstat(void)
void bdd_fprintstat(FILE *ofile)
```

Description

Prints information about the cache performance on standard output (or the supplied file). The information contains the number of accesses to the unique node table, the number of times a node was (not) found there and how many times a hash chain had to traversed. Hit and miss count is also given for the operator caches.

See also

bddCacheStat, bdd_cachestats

bdd_printtable – prints the node table entries used by a BDD

```
void bdd_printtable(BDD r)
void bdd_fprinttable(FILE* ofile, BDD r)
```

Description

Prints to either stdout or the file ofile all the entries in the main node table used by r. The format is:

```
[Nodenum] Var/level : Low High
```

Where Nodenum is the position in the node table and level is the position in the current variable order.

See also

bdd_printall, bdd_printset, bdd_printdot

bdd_relprod – relational product

#define bdd_relprod(a,b,var) bdd_appex(a,b,bddop_and,var)

Description

Calculates the relational product of a and b as a AND b with the variables in var quantified out afterwards.

Return value

The relational product or bddfalse on errors.

See also

 bdd_appex

bdd_reorder – start dynamic reordering

void bdd_reorder(int method)

Description

This function initiates dynamic reordering using the heuristic defined by method, which may be one of the following

BDD_REORDER_WIN2

Reordering using a sliding window of size 2. This algorithm swaps two adjacent variable blocks and if this results in more nodes then the two blocks are swapped back again. Otherwise the result is kept in the variable order. This is then repeated for all variable blocks.

BDD_REORDER_WIN2ITE

The same as above but the process is repeated until no further progress is done. Usually a fast and efficient method.

BDD_REORDER_WIN3

The same as above but with a window size of 3.

BDD_REORDER_WIN2ITE

The same as above but with a window size of 3.

BDD_REORDER_SIFT

Reordering where each block is moved through all possible positions. The best of these is then used as the new position. Potentially a very slow but good method.

BDD_REORDER_SIFTITE

The same as above but the process is repeated until no further progress is done. Can be extremely slow.

BDD_REORDER_RANDOM

Mostly used for debugging purpose, but may be usefull for others. Selects a random position for each variable.

See also

bdd_autoreorder, bdd_reorder_verbose, bdd_addvarblock, bdd_clrvarblocks

bdd_reorder_gain - Calculate the gain in size after a reordering

```
int bdd_reorder_gain(void)
```

Description

Returns the gain in percent of the previous number of used nodes. The value returned is

```
(100*(A-B))/A
```

Where A is previous number of used nodes and B is current number of used nodes.

bdd_reorder_hook – sets a handler for automatic reorderings

bddinthandler bdd_reorder_hook(bddinthandler handler)

Description

Whenever automatic reordering is done, a check is done to see if the user has supplied a handler for that event. If so then it is called with the argument prestate being 1 if the handler is called immediately before reordering and prestate being 0 if it is called immediately after. The default handler is bdd_default_reohandler which will print information about the reordering.

A typical handler could look like this:

```
void reorderhandler(int prestate)
{
   if (prestate)
      printf("Start reordering");
   else
      printf("End reordering");
}
```

Return value

The previous handler

See also

bdd_reorder, bdd_autoreorder, bdd_resize_hook

bddsizehandler bdd_reorder_probe(bddsizehandler handler)

Description

Reordering is typically done to minimize the global number of BDD nodes in use, but it may in some cases be usefull to minimize with respect to a specific BDD. With bdd_reorder_probe it is possible to define a callback function that calculates the size of a specific BDD (or anything else in fact). This handler will then be called by the reordering functions to get the current size information. A typical handle could look like this:

```
int sizehandler(void)
{
   extern BDD mybdd;
   return bdd_nodecount(mybdd);
}
```

No default handler is supplied. The argument handler may be NULL if no handler is needed.

Return value

The old handler

See also

bdd_reorder

bdd_reorder_verbose – enables verbose information about reorderings

int bdd_reorder_verbose(int v)

Description

With bdd_reorder_verbose it is possible to set the level of information which should be printed during reordering. A value of zero means no information, a value of one means some information and any greater value will result in a lot of reordering information. The default value is zero.

Return value

The old verbose level

See also

bdd_reorder

bdd_replace – replaces variables with other variables

BDD bdd_replace(BDD r, bddPair *pair)

Description

Replaces all variables in the BDD r with the variables defined by pair. Each entry in pair consists of a old and a new variable. Whenever the old variable is found in r then a new node with the new variable is inserted instead.

Return value

The result of the operation.

See also

bdd_newpair, bdd_setpairs

bdd_resetpair – clear all variable pairs

void bdd_resetpair(bddPair *pair)

Description

Resets the table of pairs pair by setting all substitutions to their default values (that is no change).

See also

bdd_newpair, bdd_setpair, bdd_freepair

bdd2inthandler bdd_resize_hook(bdd2inthandler handler)

Description

Whenever it is impossible to get enough free nodes by a garbage collection then the node table is resized and a test is done to see if a handler is supllied by the user for this event. If so then it is called with oldsize being the old nodetable size and newsize being the new nodetable size.

This function sets the handler to be handler. If a NULL argument is supplied then no calls are made when a table resize is done. No default handler is supplied.

Any handler should be defined like this:

```
void my_resize_handler(int oldsize, int newsize)
{
    ...
}
```

Return value

The previous handler

See also

bdd_gbc_hook, bdd_reorder_hook, bdd_setminfreenodes

bdd_restrict – restric a set of variables to constant values

```
BDD bdd_restrict(BDD r, BDD var)
```

Description

This function restricts the variables in r to constant true or false. How this is done depends on how the variables are included in the variable set var. If they are included in their positive form then they are restricted to true and vice versa. Unfortunately it is not possible to insert variables in their negated form using bdd_makeset, so the variable set has to be build manually as a conjunction of the variables. Example: Assume variable 1 should be restricted to true and variable 3 to false.

```
bdd X = make_user_bdd();
bdd R1 = bdd_ithvar(1);
bdd R2 = bdd_nithvar(3);
bdd R = bdd_addref( bdd_apply(R1,R2, bddop_and) );
bdd RES = bdd_addref( bdd_restrict(X,R) );
```

Return value

The restricted bdd.

See also

bdd_makeset, bdd_exist, bdd_forall

bdd_satcount - calculates the number of satisfying variable assignments

```
double bdd_satcount(BDD r)
double bdd_satcountset(BDD r, BDD varset)
```

Description

Calculates how many possible variable assignments there exists such that \mathbf{r} is satisfied (true). All defined variables are considered in the first version. In the second version, only the variables in the variable set **varset** are considered. This makes the function a lot slower.

Return value

The number of possible assignments.

See also

bdd_satone, bdd_fullsatone, bdd_satcountln

bdd_satcountln - calculates the log. number of satisfying variable assignments

```
double bdd_satcountln(BDD r)
double bdd_satcountlnset(BDD r, BDD varset)
```

Description

Calculates how many possible variable assignments there exists such that **r** is satisfied (true) and returns the logarithm of this. The result is calculated in such a manner that it is practically impossible to get an overflow, which is very possible for **bdd_satcount** if the number of defined variables is too large. All defined variables are considered in the first version. In the second version, only the variables in the variable set **varset** are considered. This makes the function a *lot* slower!

Return value

The logarithm of the number of possible assignments.

See also

bdd_satone, bdd_fullsatone, bdd_satcount

bdd_satone – finds one satisfying variable assignment

BDD bdd_satone(BDD r)

Description

Finds a BDD with at most one variable at each level. This BDD implies **r** and is not false unless **r** is false.

Return value

The result of the operation.

See also

bdd_allsat bdd_satoneset, bdd_fullsatone, bdd_satcount, bdd_satcountln

bdd_satoneset – finds one satisfying variable assignment

```
BDD bdd_satoneset(BDD r, BDD var, BDD pol)
```

Description

Finds a minterm in **r**. The **var** argument is a variable set that defines a set of variables that *must* be mentioned in the result. The polarity of these variables in result—in case they are undefined in **r**—are defined by the **pol** parameter. If **pol** is the false BDD then the variables will be in negative form, and otherwise they will be in positive form.

Return value

The result of the operation.

See also

bdd_allsat bdd_satone, bdd_fullsatone, bdd_satcount, bdd_satcountln

bdd_save – saves a BDD to a file

```
int bdd_fnsave(char *fname, BDD r)
int bdd_save(FILE *ofile, BDD r)
```

Description

Saves the nodes used by r to either a file ofile which must be opened for writing or to the file named fname. In the last case the file will be truncated and opened for writing.

Return value

Zero on succes, otherwise an error code from bdd.h.

See also

 $bdd \rfloor load$

bdd_scanset - returns an integer representation of a variable set

int bdd_scanset(BDD r, int **v, int *n)

Description

Scans a variable set \mathbf{r} and copies the stored variables into an integer array of variable numbers. The argument \mathbf{v} is the address of an integer pointer where the array is stored and \mathbf{n} is a pointer to an integer where the number of elements are stored. It is the users responsibility to make sure the array is deallocated by a call to $free(\mathbf{v})$. The numbers returned are guaranteed to be in ascending order.

Return value

Zero on success, otherwise a negative error code.

See also

bdd makeset

bdd_setcacheratio – Sets the cache ratio for the operator caches

int bdd_setcacheratio(int r)

Description

The ratio between the number of nodes in the nodetable and the number of entries in the operator cachetables is called the cache ratio. So a cache ratio of say, four, allocates one cache entry for each four unique node entries. This value can be set with bdd_setcacheratio to any positive value. When this is done the caches are resized instantly to fit the new ratio. The default is a fixed cache size determined at initialization time.

Return value

The previous cache ratio or a negative number on error.

See also

bdd_init

bdd_setmaxincrease - set max. number of nodes used to increase node table

int bdd_setmaxincrease(int size)

Description

The node table is expanded by doubling the size of the table when no more free nodes can be found, but a maximum for the number of new nodes added can be set with bdd_maxincrease to size nodes. The default is 50000 nodes (1 Mb).

Return value

The old threshold on succes, otherwise a negative error code.

See also

bdd_setmaxnodenum, bdd_setminfreenodes

bdd_setmaxnodenum – set the maximum available number of bdd nodes

int bdd setmaxnodenum(int size)

Description

This function sets the maximal number of bdd nodes the package may allocate before it gives up a bdd operation. The argument size is the absolute maximal number of nodes there may be allocated for the nodetable. Any attempt to allocate more nodes results in the constant false being returned and the error handler being called until some nodes are deallocated. A value of 0 is interpreted as an unlimited amount. It is *not* possible to specify fewer nodes than there has already been allocated.

Return value

The old threshold on succes, otherwise a negative error code.

See also

bdd_setmaxincrease, bdd_setminfreenodes

bdd_setminfreenodes – set min. no. of nodes to be reclaimed after GBC.

int bdd_setminfreenodes(int n)

Description

Whenever a garbage collection is executed the number of free nodes left are checked to see if a resize of the node table is required. If X = (bddfreenum * 100)/maxnum is less than or equal to n then a resize is initiated. The range of X is of course 0...100 and has some influence on how fast the package is. A low number means harder attempts to avoid resizing and saves space, and a high number reduces the time used in garbage collections. The default value is 20.

Return value

The old threshold on succes, otherwise a negative error code.

See also

bdd_setmaxnodenum, bdd_setmaxincrease

bdd_setpair – set one variable pair

```
int bdd_setpair(bddPair *pair, int oldvar, int newvar)
int bdd_setbddpair(bddPair *pair, BDD oldvar, BDD newvar)
```

Description

Adds the pair (oldvar,newvar) to the table of pairs pair. This results in oldvar being substituted with newvar in a call to bdd_replace. In the first version newvar is an integer representing the variable to be replaced with the old variable. In the second version oldvar is a BDD. In this case the variable oldvar is substituted with the BDD newvar. The possibility to substitute with any BDD as newvar is utilized in bdd_compose, whereas only the topmost variable in the BDD is used in bdd_replace.

Return value

Zero on success, otherwise a negative error code.

See also

bdd_newpair, bdd_setpairs, bdd_resetpair, bdd_replace, bdd_compose

bdd_setpairs – defines a whole set of pairs

int bdd_setpairs(bddPair *pair, int *oldvar, int *newvar, int size)
int bdd_setbddpairs(bddPair *pair, int *oldvar, BDD *newvar, int size)

Description

As for bdd_setpair but with oldvar and newvar being arrays of variables (BDDs) of size size.

Return value

Zero on success, otherwise a negative error code.

See also

bdd_newpair, bdd_setpair, bdd_replace, bdd_compose

bdd_setvarnum – set the number of used bdd variables

int bdd_setvarnum(int num)

Description

This function is used to define the number of variables used in the bdd package. It may be called more than one time, but only to increase the number of variables. The argument num is the number of variables to use.

Return value

Zero on succes, otherwise a negative error code.

See also

bdd_ithvar, bdd_varnum, bdd_extvarnum

bdd_setvarorder - set a specific variable order

void bdd_setvarorder(int *neworder)

Description

This function sets the current variable order to be the one defined by **neworder**. The parameter **neworder** is interpreted as a sequence of variable indecies and the new variable order is exactly this sequence. The array must contain all the variables defined so far. If for instance the current number of variables is 3 and **neworder** contains [1,0,2] then the new variable order is $v_1 < v_0 < v_2$.

See also

bdd_reorder, bdd_printorder

bdd_simplify – coudert and Madre's restrict function

BDD bdd_simplify(BDD f, BDD d)

Description

Tries to simplify the BDD f by restricting it to the domaine covered by d. No checks are done to see if the result is actually smaller than the input. This can be done by the user with a call to bdd_nodecount.

Return value

The simplified BDD

See also

bdd_restrict

bdd_stats - returns some status information about the bdd package

void bdd_stats(bddStat* stat)

Description

This function acquires information about the internal state of the bdd package. The status information is written into the stat argument.

See also

bddStat

bdd_strm_hook – Specifies a printing callback handler

bddstrmhandler bdd_strm_hook(bddstrmhandler handler)

Description

A printing callback handler for use with BDDs is used to convert the BDD variable number into something readable by the end user. Typically the handler will print a string name instead of the number. A handler could look like this:

```
void printhandler(ostream &o, int var)
{
    extern char **names;
    o << names[var];
}</pre>
```

The handler can then be passed to BuDDy like this: bdd_strm_hook(printhandler).

No default handler is supplied. The argument handler may be NULL if no handler is needed.

Return value

The old handler

See also

bdd_printset, bdd_file_hook, fdd_strm_hook

bdd_support – returns the variable support of a BDD

```
BDD bdd_support(BDD r)
```

Description

Finds all the variables that r depends on. That is the support of r.

Return value

A BDD variable set.

See also

 $bdd_{makeset}$

bdd_swapvar – Swap two BDD variables

int bdd_swapvar(int v1, int v2)

Description

Use bdd_swapvar to swap the position (in the current variable order) of the two BDD variables v1 and v2. There are no constraints on the position of the two variables before the call. This function may not be used together with user defined variable blocks. The swap is done by a series of adjacent variable swaps and requires the whole node table to be rehashed twice for each call to bdd_swapvar. It should therefore not be used were efficiency is a major concern.

Return value

Zero on succes and a negative error code otherwise.

See also

bdd_reorder, bdd_addvarblock

bdd_true – returns the constant true bdd

BDD bdd_true(void)

Description

This function returns the constant true bdd and can freely be used together with the bddtrue and bddfalse constants.

Return value

The constant true bdd

See also

bdd_false, bddtrue, bddfalse

bdd_unique – unique quantification of variables

BDD bdd_unique(BDD r, BDD var)

Description

Removes all occurences in **r** of variables in the set **var** by unique quantification. This type of quantification uses a XOR operator instead of an OR operator as in the existential quantification, and an AND operator as in the universal quantification.

Return value

The quantified BDD.

See also

bdd_exist, bdd_forall, bdd_makeset

bdd_var – gets the variable labeling the bdd

int bdd_var(BDD r)

Description

Gets the variable labeling the bdd r.

Return value

The variable number.

bdd_var2level - Fetch the level of a specific BDD variable

int bdd_var2level(int var)

Description

Returns the position of the variable var in the current variable order.

See also

bdd_reorder, bdd_level2var

bdd_varblockall – add a variable block for all variables

void bdd_varblockall(void)

Description

Adds a variable block for all BDD variables declared so far. Each block contains one variable only. More variable blocks can be added later with the use of bdd_addvarblock – in this case the tree of variable blocks will have the blocks of single variables as the leafs.

See also

bdd_addvarblock, bdd_intaddvarblock

bdd_varnum – returns the number of defined variables

int bdd_varnum(void)

Description

This function returns the number of variables defined by a call to bdd_setvarnum.

Return value

The number of defined variables

See also

bdd_setvarnum, bdd_ithvar

bdd_varprofile – returns a variable profile

int *bdd_varprofile(BDD r)

Description

Counts the number of times each variable occurs in the bdd r. The result is stored and returned in an integer array where the i'th position stores the number of times the i'th variable occured in the BDD. It is the users responsibility to free the array again using a call to free.

Return value

A pointer to an integer array with the profile or NULL if an error occurred.

bdd_veccompose – simultaneous functional composition

BDD bdd_veccompose(BDD f, bddPair *pair)

Description

Uses the pairs of variables and BDDs in pair to make the simultaneous substitution: $f[g_1/V_1, \ldots, g_n/V_n]$. In this way one or more BDDs may be substituted in one step. The BDDs in pair may depend on the variables they are substituting. bdd_compose may be used instead of bdd_replace but is not as efficient when g_i is a single variable, the same applies to bdd_restrict. Note that simultaneous substitution is not necessarily the same as repeated substitution. Example: $(x_1 \vee x_2)[x_3/x_1, x_4/x_3] = (x_3 \vee x_2) \neq ((x_1 \vee x_2)[x_3/x_1)][x_4/x_3] = (x_4 \vee x_2)$.

Return value

The composed BDD

See also

bdd_compose, bdd_replace, bdd_restrict

bdd_versionnum – returns the version number of the bdd package

int bdd_versionnum(void)

Description

This function returns the version number of the bdd package. The number is in the range 10-99 for version 1.0 to 9.9.

See also

bdd_versionstr

bdd_versionstr – returns a text string with version information

char* bdd_versionstr(void)

Description

This function returns a text string with information about the version of the bdd package.

See also

bdd_versionnum

bdd_xor – The logical 'xor' of two BDDs BDD bdd_xor(BDD 1, BDD r) Description This a wrapper that calls bdd_apply(1,r,bddop_xor). Return value The logical 'xor' of 1 and r. See also bdd_apply, bdd_or, bdd_and **bddfalse** – the constant false bdd extern const BDD bddfalse; Description This bdd holds the constant false value See also bddtrue, bdd_true, bdd_false **bddtrue** – the constant true bdd extern const BDD bddtrue; Description This bdd holds the constant true value See also

bddfalse, bdd_true, bdd_false

bvec – A boolean vector

```
typedef struct s_bvec
{
   int bitnum;
   BDD *bitvec;
} BVEC;

typedef BVEC bvec;
```

Description

This data structure is used to store boolean vectors. The field **bitnum** is the number of elements in the vector and the field **bitvec** contains the actual BDDs in the vector. The C++ version of **bvec** is documented at the beginning of this document

bvec_add – builds a boolean vector for addition

```
bvec bvec_add(bvec 1, bvec r)
```

Description

Builds a new boolean vector that represents the addition of two other vectors. Each element x_i in the result will represent the function

```
x_i = l_i \text{ xor } r_i \text{ xor } c_{i-1} where the carry in c_i is c_i = (l_i \text{ and } r_i) \text{ or } (c_{i-1} \text{ and } (l_i \text{ or } r_i)).
```

It is important for efficency that the BDD variables used in 1 and r are interleaved.

Return value

The result of the addition (which is already reference counted)

See also

bvec_sub, bvec_mul, bvec_shl

bvec_addref – increase reference count of a boolean vector

bvec bvec_addref(bvec v)

Description

Use this function to increase the reference count of all BDDs in a v. Please note that all boolean vectors returned from BuDDy are reference counted from the beginning.

Return value

The boolean vector v

See also

bvec_delref

bvec_coerce – adjust the size of a boolean vector

bvec bvec_coerce(int bitnum, bvec v)

Description

Build a boolean vector with bitnum elements copied from v. If the number of elements in v is greater than bitnum then the most significant bits are removed, otherwise if number is smaller then the vector is padded with constant false BDDs (zeros).

Return value

The new boolean vector (which is already reference counted)

bvec_con – Build a boolean vector representing an integer value

bvec bvec_con(int bitnum, int val)

Description

Builds a boolean vector that represents the value val using bitnum bits. The value will be represented with the LSB at the position 0 and the MSB at position bitnum-1.

Return value

The boolean vector (which is already reference counted)

See also

bvec_true, bvec_false, bvec_var

bvec_copy - create a copy of a bvec

bvec bvec_copy(bvec src)

Description

Returns a copy of src. The result is reference counted.

See also

bvec_con

bvec_delref – decrease the reference count of a boolean vector

bvec bvec_delref(bvec v)

Description

Use this function to decrease the reference count of all the BDDs in v.

Return value

The boolean vector v

See also

 $bvec_addref$

bvec_div - builds a boolean vector for division

int bvec_div(bvec 1, bvec r, bvec *res, bvec *rem)

Description

Builds a new boolean vector representing the integer division of 1 with r. The result of the division will be stored in res and the remainder of the division will be stored in rem. Both vectors should be initialized as the function will try to release the nodes used by them. If an error occurs then the nodes will not be freed.

Return value

Zero on success or a negative error code on error.

See also

bvec_mul, bvec_divfixed, bvec_add, bvec_shl

bvec_divfixed – builds a boolean vector for division by a constant

int bvec_div(bvec e, int c, bvec *res, bvec *rem)

Description

Builds a new boolean vector representing the integer division of e with c. The result of the division will be stored in res and the remainder of the division will be stored in rem. Both vectors should be initialized as the function will try to release the nodes used by them. If an error occurs then the nodes will not be freed.

Return value

Zero on success or a negative error code on error.

See also

bvec_div, bvec_mul, bvec_add, bvec_shl

bvec_equ - calculates the truth value of x = y

bdd bvec_equ(bvec 1, bvec r)

Description

Returns the BDD representing l = r (not reference counted). Both vectors must have the same number of bits.

See also

bvec_lth, bvec_lte, bvec_gth, bvec_gte, bvec_neq

bvec_false – build a vector of constant false BDDs

bvec bvec_false(int bitnum)

Description

Builds a boolean vector with bitnum elements, each of which are the constant false BDD.

Return value

The boolean vector (which is already reference counted)

See also

bvec_true, bvec_con, bvec_var

bvec_free – frees all memory used by a boolean vector

void bvec_free(bvec v)

Description

Use this function to release any unused boolean vectors. The decrease of the reference counts on the BDDs in v is done by bvec_free.

bvec_gte - calculates the truth value of $x \geq y$

bdd bvec_gte(bvec 1, bvec r)

Description

Returns the BDD representing $1 \ge r$ (not reference counted). Both vectors must have the same number of bits.

See also

bvec_lth, bvec_gth, bvec_equ, bvec_neq

bvec_gth - calculates the truth value of x > y

bdd bvec_gth(bvec 1, bvec r)

Description

Returns the BDD representing 1 > r (not reference counted). Both vectors must have the same number of bits.

See also

bvec_lth, bvec_lte, bvec_gte, bvec_equ, bvec_neq

bvec_isconst – test a vector for constant true/false BDDs

int bvec_isconst(bvec v)

Description

Returns non-zero if the vector v consists of only constant true or false BDDs. Otherwise zero is returned. This test should prelude any call to bvec_val.

See also

bvec_val, bvec_con

bvec_ite - calculates the if-then-else operator for a boolean vector

bvec bvec_ite(bdd a, bvec b, bvec c)

Description

Builds a vector where the bdd **a** has been applied bitwise to **b** and **c** in an if-then-else operation, such that the result r is:

$$r_i = ite(a, b_i, c_i);$$

Return value

The if-then-else result.

See also

bdd_ite

bvec_lte - calculates the truth value of $x \leq y$

bdd bvec_lte(bvec 1, bvec r)

Description

Returns the BDD representing $1 \le r$ (not reference counted). Both vectors must have the same number of bits.

See also

bvec_lth, bvec_gth, bvec_equ, bvec_neq

bvec_lth - calculates the truth value of x < y

bdd bvec_lth(bvec 1, bvec r)

Description

Returns the BDD representing 1 < r (not reference counted). Both vectors must have the same number of bits.

See also

bvec_lte, bvec_gth, bvec_gte, bvec_equ, bvec_neq

bvec_map1 - map a function onto a boolean vector

bvec bvec_map1(bvec a, bdd (*fun)(bdd))

Description

Maps the function fun onto all the elements in a. The value returned from fun is stored in a new vector which is then returned. An example of a mapping function is bdd_not which can be used like this

bvec res = bvec_map1(a, bdd_not)

to negate all the BDDs in a.

Return value

The new vector (which is already reference counted)

See also

bvec_map2, bvec_map3

bvec_map2 – map a function onto a boolean vector

bvec bvec_map2(bvec a, bvec b, bdd (*fun)(bdd,bdd))

Description

Maps the function fun onto all the elements in a and b. The value returned from fun is stored in a new vector which is then returned. An example of a mapping function is bdd_and which can be used like this

```
bvec res = bvec_map2(a, b, bdd_and)
```

to calculate the logical 'and' of all the BDDs in a and b.

Return value

The new vector (which is already reference counted)

See also

bvec_map1, bvec_map3

bvec_map3 – map a function onto a boolean vector

bvec bvec_map3(bvec a, bvec b, bvec c, bdd (*fun)(bdd,bdd,bdd))

Description

Maps the function fun onto all the elements in a, b and c. The value returned from fun is stored in a new vector which is then returned. An example of a mapping function is bdd_ite which can be used like this

```
bvec res = bvec_map3(a, b, c, bdd_ite)
```

to calculate the if-then-else function for each element in a, b and c.

Return value

The new vector (which is already reference counted)

See also

bvec_map1, bvec_map2

bvec_mul – builds a boolean vector for multiplication

bvec bvec_mul(bvec 1, bvec r)

Description

Builds a boolean vector representing the multiplication of 1 and r.

Return value

The result of the multiplication (which is already reference counted)

See also

bvec_mulfixed, bvec_div, bvec_add, bvec_shl

bvec_mulfixed – builds a boolean vector for multiplication with a constant

bvec bvec_mulfixed(bvec e, int c)

Description

Builds a boolean vector representing the multiplication of **e** and **c**.

Return value

The result of the multiplication (which is already reference counted)

See also

bvec_mul, bvec_div, bvec_add, bvec_shl

bvec_neq - calculates the truth value of $x \neq y$

bdd bvec_neq(bvec 1, bvec r)

Description

Returns the BDD representing $1 \neq r$ (not reference counted). Both vectors must have the same number of bits.

See also

bvec_lte, bvec_lth, bvec_gth, bvec_gth, bvec_equ

bvec_shl - shift left operation (symbolic)

bvec bvec_shl(bvec 1, bvec r, BDD c)

Description

Builds a boolean vector that represents 1 shifted \mathbf{r} times to the left. The new empty elements will be set to \mathbf{c} . The shift operation is fully symbolic and the number of bits shifted depends on the current value encoded by \mathbf{r} .

Return value

The result of the operation (which is already reference counted)

See also

bvec_add, bvec_mul, bvec_shlfixed, bvec_shr

bvec_shlfixed – shift left operation (fixed number of bits)

bvec bvec_shlfixed(bvec v, int pos, BDD c)

Description

Builds a boolean vector that represents \mathbf{v} shifted \mathbf{pos} times to the left. The new empty elements will be set to \mathbf{c} .

Return value

The result of the operation (which is already reference counted)

See also

bvec_add, bvec_mul, bvec_shl, bvec_shr

bvec_shr - shift right operation (symbolic)

bvec bvec_shr(bvec 1, bvec r, BDD c)

Description

Builds a boolean vector that represents 1 shifted r times to the right. The new empty elements will be set to c. The shift operation is fully symbolic and the number of bits shifted depends on the current value encoded by r.

Return value

The result of the operation (which is already reference counted)

See also

bvec_add, bvec_mul, bvec_shl, bvec_shrfixed

bvec_shrfixed – shift right operation

bvec bvec_shrfixed(bvec v, int pos, BDD c)

Description

Builds a boolean vector that represents v shifted pos times to the right. The new empty elements will be set to c.

Return value

The result of the operation (which is already reference counted)

See also

bvec_add, bvec_mul, bvec_shr, bvec_shl

bvec_sub – builds a boolean vector for subtraction

bvec bvec_sub(bvec 1, bvec r)

Description

Builds a new boolean vector that represents the subtraction of two other vectors. Each element x_i in the result will represent the function

$$x_i = l_i \text{ xor } r_i \text{ xor } c_{i-1}$$

where the carry in c_i is

$$c_i = (l_i \text{ and } r_i \text{ and } c_{i-1}) \text{ or } (\text{not } l_i \text{ and } (r_i \text{ or } c_{i-1})).$$

It is important for efficency that the BDD variables used in 1 and r are interleaved.

Return value

The result of the subtraction (which is already reference counted)

See also

bvec_add, bvec_mul, bvec_shl

bvec_true – build a vector of constant true BDDs

bvec bvec_true(int bitnum)

Description

Builds a boolean vector with bitnum elements, each of which are the constant true BDD.

Return value

The boolean vector (which is already reference counted)

See also

bvec_false, bvec_con, bvec_var

bvec_val - calculate the integer value represented by a boolean vector

int bvec_val(bvec v)

Description

Calculates the value represented by the bits in v assuming that the vector v consists of only constant true or false BDDs. The LSB is assumed to be at position zero.

Return value

The integer value represented by v.

See also

bvec_isconst, bvec_con

bvec_var – build a boolean vector with BDD variables

bvec bvec_var(int bitnum, int offset, int step)

Description

Builds a boolean vector with the BDD variables v_1, \ldots, v_n as the elements. Each variable will be the the variabled numbered offset + N*step where N ranges from 0 to bitnum-1.

Return value

The boolean vector (which is already reference counted)

See also

bvec_true, bvec_false, bvec_con

bvec_varfdd – build a boolean vector from a FDD variable block

bvec bvec_varfdd(int var)

Description

Builds a boolean vector which will include exactly the variables used to define the FDD variable block var. The vector will have the LSB at position zero.

Return value

The boolean vector (which is already reference counted)

See also

bvec_var

bvec_varvec – build a boolean vector with the variables passed in an array

bvec bvec_varvec(int bitnum, int *var)

Description

Builds a boolean vector with the BDD variables listed in the array var. The array must be of size bitnum.

Return value

The boolean vector (which is already reference counted)

See also

 $bvec_var$

fdd_clearall - clear all allocated FDD blocks

void fdd_clearall(void)

Description

Removes all defined finite domain blocks defined by fdd_extdomain() and fdd_overlapdomain()

fdd_domain - BDD encoding of the domain of a FDD variable

BDD fdd_domain(int var)

Description

Returns what corresponds to a disjunction of all possible values of the variable var. This is more efficient than doing fdd_ithvar(var,0) OR fdd_ithvar(var,1) ... explicitely for all values in the domain of var.

Return value

The encoding of the domain

fdd_domainnum - number of defined finite domain blocks

int fdd_domainnum(void)

Description

Returns the number of finite domain blocks define by calls to bdd_extdomain.

Return value

The number of defined finite domain blocks or a negative error code

See also

fdd_domainsize, fdd_extdomain

fdd_domainsize - real size of a finite domain block

int fdd_domainsize(int var)

Description

Returns the size of the domain for the finite domain block var.

Return value

The size or a negative error code

See also

fdd_domainnum

fdd_equals - returns a BDD setting two FD. blocks equal

BDD fdd_equals(int f, int g)

Description

Builds a BDD which is true for all the possible assignments to the variable blocks f and g that makes the blocks equal. This is more or less just a shorthand for calling fdd_equ().

Return value

The correct BDD or the constant false on errors.

fdd_extdomain - adds another set of finite domain blocks

int fdd_extdomain(int *dom, int num)

Description

Extends the set of finite domain blocks with the num domains in dom. Each entry in dom defines the size of a new finite domain which later on can be used for finite state machine traversal and other operations on finte domains. Each domain allocates $\log_2(|dom[i]|)$ BDD variables to be used later. The ordering is interleaved for the domains defined in each call to bdd_extdomain. This means that assuming domain D_0 needs 2 BDD variables x_1 and x_2 , and another domain D_1 needs 4 BDD variables y_1, y_2, y_3 and y_4 , then the order will be $x_1, y_1, x_2, y_2, y_3, y_4$. The index of the first domain in dom is returned. The index of the other domains are offset from this index with the same offset as in dom.

The BDD variables needed to encode the domain are created for the purpose and do not interfere with the BDD variables already in use.

Return value

The index of the first domain or a negative error code.

See also

fdd_ithvar, fdd_equals, fdd_overlapdomain

fdd_file_hook - Specifies a printing callback handler

bddfilehandler fdd_file_hook(bddfilehandler handler)

Description

A printing callback handler for use with FDDs is used to convert the FDD integer identifier into something readable by the end user. Typically the handler will print a string name instead of the identifier. A handler could look like this:

```
void printhandler(FILE *o, int var)
{
   extern char **names;
   fprintf(o, "%s", names[var]);
}
```

The handler can then be passed to BuDDy like this: fdd_file_hook(printhandler).

No default handler is supplied. The argument handler may be NULL if no handler is needed.

Return value

The old handler

See also

fdd_printset, bdd_file_hook

fdd_intaddvarblock – adds a new variable block for reordering

int fdd_intaddvarblock(int first, int last, int fixed)

Description

Works exactly like bdd_addvarblock except that fdd_intaddvarblock takes a range of FDD variables instead of BDD variables.

Return value

Zero on success, otherwise a negative error code.

See also

bdd_addvarblock, bdd_intaddvarblock, bdd_reorder

fdd_ithset - the variable set for the i'th finite domain block

BDD fdd_ithset(int var)

Description

Returns the variable set that contains the variables used to define the finite domain block var.

Return value

The variable set or the constant false BDD on error.

See also

 fdd_ithvar

fdd_ithvar - the BDD for the i'th FDD set to a specific value

BDD fdd_ithvar(int var, int val)

Description

Returns the BDD that defines the value val for the finite domain block var. The encoding places the Least Significant Bit at the top of the BDD tree (which means they will have the lowest variable index). The returned BDD will be $V_0 \wedge V_1 \wedge \ldots \wedge V_N$ where each V_i will be in positive or negative form depending on the value of val.

Return value

The correct BDD or the constant false BDD on error.

See also

 fdd_ithset

fdd_makeset - creates a variable set for N finite domain blocks

BDD fdd_makeset(int *varset, int varnum)

Description

Returns a BDD defining all the variable sets used to define the variable blocks in the array varset. The argument varnum defines the size of varset.

Return value

The correct BDD or the constant false on errors.

See also

fdd_ithset, bdd_makeset

fdd_overlapdomain - combine two FDD blocks into one

int fdd_overlapdomain(int v1, int v2)

Description

This function takes two FDD blocks and merges them into a new one, such that the new one is encoded using both sets of BDD variables. If v1 is encoded using the BDD variables a_1, \ldots, a_n and has a domain of $[0, N_1]$, and v2 is encoded using b_1, \ldots, b_n and has a domain of $[0, N_2]$, then the result will be encoded using the BDD variables $a_1, \ldots, a_n, b_1, \ldots, b_n$ and have the domain $[0, N_1 * N_2]$. The use of this function may result in some strange output from fdd_printset.

Return value

The index of the finite domain block

See also

fdd_extdomain

fdd_printset - prints a BDD for a finite domain block

```
void fdd_printset(BDD r)
void fdd_fprintset(FILE *ofile, BDD f)
```

Description

Prints the BDD f using a set notation as in bdd_printset but with the index of the finite domain blocks included instead of the BDD variables. It is possible to specify a printing callback function with fdd_file_hook or fdd_strm_hook which can be used to print the FDD identifier in a readable form.

See also

bdd_printset, fdd_file_hook, fdd_strm_hook

fdd_scanallvar - Finds one satisfying value of all FDD variables

int* fdd_scanallvar(BDD r)

Description

Finds one satisfying assignment in r of all the defined FDD variables. Each value is stored in an array which is returned. The size of this array is exactly the number of FDD variables defined. It is the user's responsibility to free this array using free().

Return value

An array with all satisfying values. If r is the trivially false BDD, then NULL is returned.

See also

 $fdd_scanvar$

fdd_scanset – scans a variable set

int fdd_scanset(BDD r, int **varset, int *varnum)

Description

Scans the BDD r to find all occurences of FDD variables and then stores these in varset. varset will be set to point to an array of size varnum which will contain the indices of the found FDD variables. It is the users responsibility to free varset after use.

Return value

Zero on success or a negative error code on error.

See also

 $fdd_{makeset}$

fdd_scanvar - Finds one satisfying value of a FDD variable

int fdd_scanvar(BDD r, int var)

Description

Finds one satisfying assignment of the FDD variable var in the BDD r and returns this value.

Return value

The value of a satisfying assignment of var. If r is the trivially false BDD, then a negative value is returned.

See also

 $fdd_scanallvar$

fdd_setpair - defines a pair for two finite domain blocks

int fdd_setpair(bddPair *pair, int p1, int p2)

Description

Defines each variable in the finite domain block p1 to be paired with the corresponding variable in p2. The result is stored in pair which must be allocated using bdd_makepair.

Return value

Zero on success or a negative error code on error.

See also

fdd_setpairs

fdd_setpairs - defines N pairs for finite domain blocks

int fdd_setpairs(bddPair *pair, int *p1, int *p2, int size)

Description

Defines each variable in all the finite domain blocks listed in the array p1 to be paired with the corresponding variable in p2. The result is stored in pair which must be allocated using bdd_makeset.

Return value

Zero on success or a negative error code on error.

See also

bdd_setpair

fdd_strm_hook - Specifies a printing callback handler

bddstrmhandler fdd_strm_hook(bddstrmhandler handler)

Description

A printing callback handler for use with FDDs is used to convert the FDD integer identifier into something readable by the end user. Typically the handler will print a string name instead of the identifier. A handler could look like this:

```
void printhandler(ostream &o, int var)
{
   extern char **names;
   o << names[var];
}</pre>
```

The handler can then be passed to BuDDy like this: fdd_strm_hook(printhandler).

No default handler is supplied. The argument handler may be NULL if no handler is needed.

Return value

The old handler

See also

fdd_printset, bdd_file_hook

fdd_varnum – binary size of a finite domain block

```
int fdd_varnum(int var)
```

Description

Returns the number of BDD variables used for the finite domain block var.

Return value

The number of variables or a negative error code

See also

 fdd_{vars}

fdd_vars - all BDD variables associated with a finite domain block

int *fdd_vars(int var)

Description

Returns an integer array containing the BDD variables used to define the finite domain block var. The size of the array is the number of variables used to define the finite domain block. The array will have the Least Significant Bit at pos 0. The array must not be deallocated.

Return value

Integer array containing the variable numbers or NULL if v is an unknown block.

See also

 fdd_varnum

operator<< - C++ output operator for BDDs</pre>

```
ostream &operator<<(ostream &o, const bdd_ioformat &f)
ostream &operator<<(ostream &o, const bdd &r)</pre>
```

Description

BDDs can be printed in various formats using the C++ iostreams library. The formats are the those used in bdd_printset, bdd_printtable, fdd_printset and bdd_printdot. The format can be specified with the following format objects:

bddset	BDD level set format
bddtable	BDD level table format
bdddot	Output for use with Dot
bddall	The whole node table
fddset	FDD level set format

So a BDD x can for example be printed as a table with the command

```
cout << bddtable << x << endl.
```

Return value

The specified output stream

See also

bdd_strm_hook, fdd_strm_hook

Bibliography

- [1] Randal E. Bryant. Graph-Based Algorithms for Boolean Function Manipulation. *IEEE Transactions on Computers*, C-35(8):677–691, August 1986.
- [2] Randal E. Bryant. Symbolic Boolean manipulation with ordered binary decision diagrams. *ACM Computing Surveys*, 24(3):293–318, September 1992.
- [3] K.S. Brace, R.L. Rudell, and R.E. Bryant. Efficient Implementation of a BDD Package. In 27th ACM/IEEE Design Automation Conference, pages 40–45, Orlando, Florida, June 1990. ACM/IEEE, IEEE Computer Society Press.
- [4] R. Rudell. Dynamic Variable Ordering for Ordered Binary Decision Diagrams. In *IEEE /ACM International Conference on CAD*, pages 42–47, Santa Clara, California, November 1993. ACM/IEEE, IEEE Computer Society Press.

Index

addition, 8	bdd_gbc_hook , 37
arithmetic, 7	bdd_getallocnum, 37
arrimmente, r	bdd_getnodenum, 38
bdd_addref , 22	bdd_getreorder_method, 38
bdd_addvarblock, 23	bdd_getreorder_times, 38
bdd_allsat , 24	bdd_high, 39
bdd_and, 24	_ :
bdd_anodecount, 25	bdd_ibuildcube, 29
bdd_appall, 25	bdd_imp , 39
bdd_appex, 26	bdd_init, 40
bdd_apply, 27	bdd_intaddvarblock, 23
bdd_appuni, 27	bdd_isrunning, 40
bdd_autoreorder, 28	bdd_ite , 41
bdd_autoreorder_times, 28	bdd_ithvar, 41
bdd_biimp, 28	bdd_level2var, 42
bdd_blockfile_hook, 29	bdd_load , 42
bdd_buildcube, 29	bdd_low, 43
bdd_cachestats, 30	bdd_makeset, 43
•	bdd_newpair, 44
bdd_clear_error, 30 bdd_clrvarblocks, 30	bdd_nithvar, 44
•	bdd_nodecount, 45
bdd_compose, 31	bdd_not , 45
bdd_constrain, 31	bdd_or , 45
bdd_delref, 32	$bdd_pathcount$, 46
bdd_disable_reorder, 32	$bdd_printall$, 46
bdd_done, 32	bdd_printdot, 47
bdd_enable_reorder, 33	$bdd_printorder$, 47
bdd_error_hook, 33	bdd_printset, 48
bdd_errstring, 34	bdd_printstat, 48
bdd_exist, 34	$bdd_printtable$, 49
bdd_extvarnum, 34	$\operatorname{bdd_relprod}$, 49
bdd_false, 35	$bdd_reorder$, 50
bdd_file_hook, 35	$bdd_{reorder_gain}$, 51
bdd_fnload , 42	${\it bdd_reorder_hook}$, 51
bdd_fnsave, 57	${\it bdd_reorder_probe}$, 52
bdd_forall, 36	${\it bdd_reorder_verbose}$, 52
bdd_fprintall, 46	$bdd_replace$, 53
bdd_fprintdot, 47	bdd_resetpair, 53
bdd_fprintset, 48	bdd_resize_hook, 54
bdd_fprintstat, 48	bdd_restrict, 55
bdd_fprinttable, 49	bdd_satcount, 55
${\it bdd_freepair} \;, 36$	$bdd_satcountln$, 56
$\operatorname{bdd_fullsatone}$, 36	bdd_satone, 56
	,

$bdd_satoneset$, 57	$bvec_gth$, 73
bdd_save, 57	bvec_isconst, 74
bdd_scanset, 58	bvec_ite, 74
bdd_setbddpair , 60	bvec_lte, 74
bdd_setbddpairs, 61	bvec_lth, 75
bdd_setcacheratio, 58	$bvec_map1$, 75
bdd_setcountlnset, 56	$bvec_map2$, 76
bdd_setcountset, 55	$bvec_map3$, 76
bdd_setmaxincrease, 59	bvec_mul, 77
bdd_setmaxnodenum, 59	bvec_mulfixed, 77
bdd_setminfreenodes, 60	bvec_neq, 77
bdd_setpair, 60	bvec_shl , 78
bdd_setpairs, 61	bvec_shlfixed, 78
bdd_setvarnum, 61	bvec_shr , 79
bdd_setvarorder, 62	bvec_shrfixed, 79
bdd_simplify, 62	bvec_sub, 80
bdd_stats, 62	bvec_true, 80
bdd_strm_hook, 63	bvec_val, 81
bdd_support, 63	bvec_var, 81
bdd_swapvar , 64	bvec_varfdd, 82
bdd_true, 64	bvec_varvec, 82
bdd_unique, 65	
bdd_{var} , 65	C++ interface, 6
$bdd_var2level$, 65	compiling, 3
$\operatorname{bdd_varblockall}$, 66	demania vaniable needening 5
$\operatorname{bdd_varnum}$, 66	dynamic variable reordering, 5
$\operatorname{bdd_varprofile}$, 66	error handling, 6
$bdd_veccompose$, 67	
$bdd_versionnum$, 67	$fdd_clearall$, 82
$bdd_versionstr$, 67	fdd_domain , 83
bdd_xor , 68	$fdd_domainnum$, 83
bddCacheStat, 20	$fdd_domainsize$, 83
bddfalse, 68	fdd_equals , 84
${\it bddGbcStat}$, 21	$fdd_{extdomain}$, 84
$\mathrm{bddStat}$, 22	fdd_file_hook , 85
$bddtrue\;,\;68$	$fdd_fprintset$, 88
Boolean Vectors, 7	$fdd_intaddvarblock$, 85
bvec , 69	fdd_ithset , 86
$bvec_add$, 69	fdd_{ithvar} , 86
$bvec_addref$, 70	$fdd_{makeset}$, 87
bvec_coerce, 70	$fdd_overlapdomain$, 87
$bvec_con$, 70	$fdd_printset$, 88
bvec_copy , 71	$fdd_scanallvar$, 88
$bvec_delref$, 71	$fdd_scanset$, 89
$bvec_div$, 71	$fdd_scanvar$, 89
bvec_divfixed , 72	$fdd_setpair$, 90
bvec $_{equ}$, 72	$fdd_setpairs$, 90
$bvec_false$, 72	fdd_strm_hook , 91
$bvec_free$, 73	fdd_varnum , 91
$bvec_gte$, 73	fdd_{vars} , 92

finite domain blocks, 7

 $\begin{array}{c} \text{implementation, } 13 \\ \text{installing, } 3 \end{array}$

operator<< , 92

programming examples, 3

relational product, 26 reordering, 5

variable reordering, 5 variable sets, 4